Clans, Guilds, and Markets:
Apprenticeship Institutions and Growth
in the Pre-Industrial Economy*

David de la Croix
Univ. cath. Louvain

Matthias Doepke
Northwestern

Joel Mokyr
Northwestern

March 2016

Abstract

In the centuries leading up to the Industrial Revolution, Western Europe gradually pulled ahead of other world regions in terms of technological creativity, population growth, and income per capita. We argue that superior institutions for the creation and dissemination of productive knowledge help explain the European advantage. We build a model of technological progress in a pre-industrial economy that emphasizes the person-to-person transmission of tacit knowledge. The young learn as apprentices from the old. Institutions such as the family, the clan, the guild, and the market organize who learns from whom. We argue that medieval European institutions such as guilds, and specific features such as journeymanship, can explain the rise of Europe relative to regions that relied on the transmission of knowledge within extended families or clans.

1 Introduction

The intergenerational transmission of skills and more generally of "knowledge how" has been central to the functioning of all economies since the emergence of agriculture. Historically, this knowledge was almost entirely "tacit" knowledge, in the standard sense used today in the economics of knowledge literature (Cowan and Foray, 1997; Foray, 2004, pp. 71–73, 96–98). Although economic historians have long recognized its the importance for the functioning of the economy (Dunlop, 1911, 1912), it is only more recently that tacit knowledge has been explicitly connected with the literature on human capital and its role in the Industrial Revolution and the emergence of modern economic growth (Humphries, 2003, 2010; Kelly, Mokyr, and Ó Gráda, 2014). The main mechanism through which tacit skills were transmitted across individuals was apprenticeship, a relation linking a skilled adult to a youngster whom he taught the trade. The literature on the economics of apprenticeship has focused on a number of topics we shall discuss in some detail below. Yet little has been done to analyze apprenticeship as a global phenomenon, organized in different modes.

In this paper, we examine the role of apprenticeship institutions in explaining economic growth in the pre-industrial era. We build a model of technological progress that emphasizes the person-to-person transmission of tacit knowledge from the old to the young (as in Lucas 2009 and Lucas and Moll 2014). Doing so allows us to go beyond the simplified representations of technological progress used in existing models of pre-industrial growth, such as Galor (2011). In our setup, a key part is played by institutions—the family, the clan, the guild, and the market—which organize who learns from whom. We argue that the archetypes of modes of apprenticeship that we consider in the model, while abstract, can be mapped into actual institutions that were prevalent throughout history in different world regions.

We use the theory to address a central question about pre-industrial growth, namely why Western Europe surpassed other regions in technological progress and growth in the centuries leading up to industrialization. In particular, we claim that medieval European institutions such as guilds, with specific features such as journeymanship, were critical in speeding up the dissemination of new productive knowledge in Europe, compared to regions that relied on the transmission of knowledge within extended families or clans.[1]

---

[1] Our emphasis on the role of clans in organizing economic life for comparative development is shared with Greif and Tabellini (2010), although the mechanisms considered are entirely different.

Before developing a theory of the modes of institutional organization of apprenticeship and their implications for knowledge dissemination, we address three key issues one should address in modeling. First, the main issue is the extent to which the mode of organizing the transmission of skills was consistent with technological progress. We take the view from the outset that all systems of apprenticeship are consistent with at least some degree of progress. Even when the system has strong conservative elements that administer rigid tests on the existing procedures and techniques, learning by doing generates a certain cumulative drift over time that can raise productivity, even in the most conservative systems. That said, the rates at which innovation occurred within artisanal systems have differed dramatically over time, over different societies and even between different products. Differences in rates of technological progress may in principle have two different sources, namely the rate of original innovation and the speed of the dissemination of existing ideas. While we discuss implications for original innovation, our theoretical analysis focuses on the second channel. Specifically, we ask how conducive the intergenerational transmission mechanism was to the dissemination of best-practice techniques, and how conducive an apprenticeship system based on personal contacts and mostly local networks was to closing gaps between best-practice and average-practice techniques.

Second, the training contract between master and apprentice (whether formal or implicit), for obvious reasons, represents a complicated transaction. For one thing, unless that transmission occurs within the nuclear family (in a father-son line), the person negotiating the transaction is not the subject of the contract himself but his parents, raising inevitable agency problems. Moreover, the contract written with the "master" by its very nature is largely incomplete. The details of what is to be taught, how well, how fast, what tools and materials the pupil would be allowed to use, as well as other aspects such as room and board, are impossible to specify fully in advance. Equally, apart from a flat fee that many apprentices paid upfront, the other services rendered by the apprentice, such as labor, were hard to enumerate. This was, in a word, an archetypical incomplete contract. As a consequence, in our theoretical analysis moral hazard in the master-apprentice relationship is the central element that creates a need for institutions to organize the transmission of knowledge.

Third, and as a result of the contractual problems in writing an apprenticeship agreement, a variety of institutional setups for supervising and arbitrating the apprentice-master relations can be found in the past. In all cases except direct parent-child rela-

tionships, some kind of enforcement mechanism was required. Basically three types of institutions can be discerned that enforced contracts and, as a result, ended up regulating the industry in some form. They were (1) informal institutions, based on reputation and trust; (2) non-state semi-formal institutions (guilds, local authorities such as the Dutch *neringen*); and (3) third party (state) enforcement usually by local authorities and courts. In many places all three worked simultaneously and should be regarded as complements, but their relative importance varied quite a bit. In our theoretical analysis, we map the wide variety of historical institutions into four archetypes, namely the (nuclear) family, the clan (i.e., a trust-based institution comprising an extended family), the guild (a semi-formal institution), and the market (which comprises formal contract enforcement by a third party).

Our theoretical model builds on a recent literature in the theory of economic growth that puts the spotlight on the dissemination of knowledge through the interpersonal exchange of ideas.[2] Given our focus on pre-industrial growth, the analysis is carried out in a Malthusian setting with endogenous population growth in which the factors of production are the fixed factor land and the supply of effective labor by workers ("craftsmen") in a variety of trades. Knowledge is represented as the efficiency with which craftsmen perform tasks. While there is some scope for new innovation, the main engine of technological progress is the transmission of productive knowledge from old to young workers. Young workers learn from elders through a form of apprenticeship. There is a distribution of knowledge (or productivity) across workers, and when young workers learn from multiple old workers, they can adopt the best technique to which they have been exposed. Through this process, average productivity in the economy increases over time.[3]

The central features of our analysis are that the transmission of knowledge (teaching)

---

[2] Specifically, the underlying engine of growth in our model is closely related to Lucas (2009), who in turn builds on earlier seminal contributions by Jovanovic and Rob (1989), Kortum (1997), and Eaton and Kortum (1999). Earlier explicit models of endogenous technological progress build on R&D efforts by firms, following the seminal papers of Romer (1990) and Aghion and Howitt (1992). While such models are useful for analyzing innovation in modern times, their applicability to pre-industrial growth is doubtful, partly because legal protections for intellectual property became widespread only recently.

[3] Recent growth models that build on a process of this kind (in addition to Lucas 2009) include Alvarez, Buera, and Lucas (2008, 2013), König, Lorenz, and Zilibotti (2015), Lucas and Moll (2014), Luttmer (2007, 2015), and Perla and Tonetti (2014). Among these papers, Luttmer (2015) also considers a market environment where students are matched to teachers, although without allowing for different institutions. Particularly relevant to our work is also Fogli and Veldkamp (2012), where the structure of a network has important ramifications for the rate of productivity growth. The research is also related to models of productivity growth over the very long run such as Kremer (1993) and Jones (2001).

requires effort on the part of the master; that this leads to a moral hazard problem in the master-apprentice relationship; and that, as a consequence, institutions that mitigate or eliminate the moral hazard problem are key determinants of the dissemination of knowledge and economic growth.[4]

The "family" in our analysis is the polar case where no enforcement mechanism is available that reaches beyond the nuclear family, and hence children learn only from their own parents. In the family equilibrium, there is still some technological progress due to experimentation with new ideas and innovation within the family, but there is no dissemination of knowledge, and hence the rate of technological progress is low. The "clan" is an extended family where reputation and trust provide an informal enforcement mechanism. Hence, children can become apprentices of members of the clan other than their own parents (such as aunts or uncles). The clan equilibrium leads to faster technological progress compared to the family equilibrium, because productive new ideas disseminate within each clan. The "guild" in our model is a coalition of all the masters in a given trade that provides a semi-formal enforcement mechanism, but also regulates (monopolizes) apprenticeship within the trade. Finally, the "market" is a formal enforcement institution where an outside authority (such as the state) enforces contracts, and in addition, rules are in place that prevent anticompetitive behavior (such limitations on the supply of apprenticeship imposed by guilds).

In terms of mapping the model into historical institutions, we regard most world regions (in particular China, India, and the Middle East) as being characterized by the clan equilibrium throughout the pre-industrial era. Here extended families organized most aspects of economic life, including the transmission of skills between generations. The distinctive features of Western Europe are a much larger role of the nuclear family from the first centuries of the Common Era; little significance of extended families; and an increasing relevance of institutions that do not rely on family ties (such as cities and indeed guilds) starting in the Middle Ages. Hence, in the language of the model, we view Western Europe as undergoing a transition from the family to the guild equilibrium during the Middle Ages, and onwards to the market equilibrium in the centuries leading up to the Industrial Revolution.

To explain the emerging primacy of Western Europe over other world regions, we look to the comparative growth performance of the clan and guild institutions. Both the

---

[4]Additional innovations relative to the recent literature on growth based on the exchange of ideas are that we examine endogenous institutional change, and that we allow for endogenous population growth.

clan and the guild provided for apprenticeship outside the nuclear family, and a count against the guild is the anticompetitive nature of guilds, i.e., the possibility that guilds limited access to apprenticeship to raise prices. However, our analysis identifies a much more important force that explains why the Western European system of knowledge acquisition came to dominate. Namely, apprenticeship within guilds was independent of family ties, and thus allowed for dissemination of knowledge in the entire economy, whereas in a clan based system the dissemination of knowledge was impaired. A different side of the same coin is that in a clan based system, relatively little is gained by learning from multiple elders, because given that these elders belong to the same clan, they are likely to have received the same training and thus to have very similar knowledge. In contrast, in a guild (and also in the market) family ties do not limit apprenticeship, and hence the young can sample from a much wider variety of knowledge, implying that apprenticeship is more productive and knowledge disseminates more quickly. The historical evidence shows that, indeed, in Europe master and apprentice were far less likely to be related to each other than elsewhere. Moreover, the guild system sometimes included specific features, in particular journeymanship, that had the effect of providing access to a broader range of knowledge and fostering the spread of new techniques and ideas. In a narrower system based on blood relationships, such a wide exchange of ideas was not feasible.

Our framework can also be used to explore why institutional change (i.e., the adoption of guilds and, later on, the market) took place in Europe, but not elsewhere. If adopting new institutions is costly, the incentive to adopt will be lower when the initial economic system is relatively more successful, i.e., in a clan-based economy compared to a family-based economy. If the cost of adopting new institutions declines with population density, it is possible that new institutions will only be adopted if the economy starts out in the family equilibrium, but not if the clan equilibrium is the initial condition. We also discuss complementary mechanisms (going beyond the formal model) that are likely to have contributed also to faster institutional change in Europe.

The paper engages three recent literatures in economic history that have received considerable attention. One is the debate over whether craft guilds were on balance a hindrance to technological progress, or whether they stimulated it by supporting apprenticeship relations (for a recent summary, see van Zanden and Prak, eds. 2013b and Ogilvie 2004). The second new literature is the one emphasizing the ingenuity of artisans and skilled workers in generating knowledge, and minimizing the classic distinc-

tion between formal science and practical knowledge. Roberts and Schaffer stress the importance of "local technological projects" carried out by the "tacit genius of on-the-spot practitioners;" here they clearly refer to thoughtful and well-trained artisans who advance the frontiers of useful knowledge (Roberts and Schaffer, 2007; see also Long 2011). Little in this literature, however, has focused on the intergenerational transmission of the knowledge embedded in such "mindful hands" through the institutions of apprenticeship. The third literature is concerned with understanding economic, institutional, and cultural differences between Europe and other world regions as a source of of the relative rise of Europe and decline of other regions in the centuries leading up to the Industrial Revolution (e.g., Voigtländer and Voth 2013b, 2013a). We build in particular on the work by Greif and Tabellini (2015) on the role of clans in China versus "corporations" in Europe (i.e., formal organizations that exist independently of family ties) for sustaining cooperation (see also Greif 2006 and Greif, Iyigun, and Sasson 2012). However, Greif and Tabellini do not consider the implications of such institutions for the generation and dissemination of productive knowledge.

The paper is organized as follows. Section 2 describes key historical aspects of apprenticeship systems on which we base our theory. Our formal model of knowledge growth is described in Section 3. Section 4 analyzes the different apprenticeship institutions and derives their implications for economic growth. Section 5 makes use of theoretical results to analyze the rise of European technological primacy, and considers endogenous adoption of institutions. Section 6 concludes.

2 Historical Background

2.1 Learning on the Shopfloor

Through most of history, the acquisition of human capital took the form, in the felicitous phrase of De Munck and Soly (2007), of "learning on the shopfloor." One should not take this too literally: some skills had to be learned on board of ships or on the bottom of coal mines. Yet it remains true that learning took place through personal contact between a designated "master" and his apprentice.[5] As they point out (ibid., p. 6), before the middle of the nineteenth century there were few alternatives to acquiring useful productive skills. Some of the better schools, such as Britain's dissenting academies or the drawing

---

[5]We consider an era which is characterized by a sharp division of labor by gender, and where formal apprenticeship generally was open only to boys. Hence, we will refer to master and apprentice as "he" throughout the paper, and our model does not distinguish two genders.

6

schools that emerged on the European continent around 1600, taught, in addition to the three R's, some useful skills such as draftmanship, chemistry, and geography. But on the whole, the one-on-one learning process was the one experienced by most.[6]

The economics of apprenticeship in the premodern world is based on the insight that each master artisan basically produced a set of two connected outputs: a commodity or service, and new craftsmen. In other words, he sold "human capital." The economics of such a setup explains many of the historical features of the system. The best-known, of course, is that the apprentice had to supply labor services to the master in partial payment for his training and his room and board. In some instances, this component became so large that the apprentice contract was more of a labor contract than a training arrangement.[7] Such provisions underline the basic idea of joint production, in which the two activities—production and training—were strongly complementary.

As Humphries (2003) has pointed out, the contract between the master and the apprentice in any institutional setting is problematic in two ways. First, the flows of the services transacted for is non-synchronic (although the exact timing differed from occupation to occupation). Second, these flows cannot be fully specified ex ante or observed ex post. The apprentice, by the very nature of the teaching process, is not in a position to assess adequately whether he has received what he has paid for until the contract is terminated. Even if the apprentice himself could observe the implementation of the contract, the details would be unverifiable for third parties and adjudicators. Because the transaction is non-repeated, the party who receives the services or payment first has an incentive to shirk. This is known ex ante, and therefore it is possible that the transaction does not take place and that the economy would suffer from the serious underproduction of training.[8] However, since that would mean that intergenerational transmission of knowledge would take place exclusively within families, some societies have come up with institutions that allowed the contracts to be enforced between unrelated parties.

---

[6]Of course, printed material became increasingly widespread after Gutenberg, but played a limited role in the training of craftsmen. The printing press was relatively more important for providing access to science and and similar "top end" knowledge; see Dittmar (2011) for an analysis of the overall impact of printing on early economic growth.

[7]Steffens (2001), pp. 124–25, observes on the basis of nineteenth century Belgian apprentices that little explicit teaching was carried out and that the learning was simply occurring through the performance of tasks.

[8]The suggestion by Epstein (2008, p. 61) that the contract could be rewritten to prevent either side from defaulting is not persuasive. For instance, he suggests that by backloading some of the payments from master to apprentice, the latter would be deterred from defecting early—but that of course just shifts the opportunity to cheat from the apprentice to the master.

These institutions curbed opportunistic behavior in different ways, but they all required some kind of credible punishment. As we will see in our theoretical analysis below, the more sophisticated and effective institutions led to better quality of training (in a precise matter we will define) and thus led to faster technological progress.

2.2 Apprenticeship in Western Europe

The evidence suggests that at least in early modern Europe the market for apprenticeship functioned reasonably well, despite the obvious dangers of market failure. A good indicator of the working of the market for human capital, at least in Britain, was the premium that parents paid to a master. Occupations that demanded more skill and promised higher lifetime earnings commanded higher premiums. The differences in premiums meant that this market worked, in the sense that the apprenticeship premium seems to have varied positively with the expected profitability and prestige of the chosen occupation (Brooks 1994, p. 60). As noted by Minns and Wallis (2013), the premium paid was not a full payment equal to the present value of the training plus room and board, which usually were much higher than the upfront premium. The rest normally was paid in kind with the labor provided by the apprentice. The premium served more than one purpose. In part, it was to insure the master against the risk of an early departure of the apprentice. But in part it reflected also the quality of the training and the cost to the master, as well as its scarcity value (ibid., p. 340). More recently, it has been shown that the premium worked as a market price reflecting rising and falling demand for certain occupations resulting from technological shocks (Ben Zeev, Mokyr, and Van Der Beek 2015). It is telling that not all apprentices paid the premiums: whereas 74 percent of engravers in London paid a premium in London, only 17 percent of blacksmiths did (Minns and Wallis, 2013, p. 344). If an impecunious apprentice could not pay, he had the option of committing to a longer indenture, as was the case in seventeenth century Vienna (Steidl, 2007, p. 143). In eighteenth century Augsburg a telling example is that a "big strong man was often taken on without having to pay any apprenticeship premium, whereas a small weak man would have to pay more." It is also recorded that apprentices with poor parents who could not afford the premium would end up being trained by a master who did inferior work (Reith, 2007, p.183). This market worked in sophisticated ways, and it is clear is that human capital was recognized to be a valuable commodity. The formal contract signed by the apprentice in the seventeenth century included a commitment to protect the master's secrets and not to abscond, as well as to not commit fornication (Smith, 1973, p. 150).

The precise operation of apprenticeship varied a great deal. The duration of the contract depended above all on the complexity of the trade to be learned, but also on the age at which youngsters started their apprenticeship. On the continent three to four years seems to have been the norm (De Munck and Soly, 2007, p. 18). As would perhaps be expected, there is evidence that the duration of contracts grew over the centuries as techniques became more complex and the division of labor more specialized as a result of technological progress (Reith 2007, p. 183).

To what extent was the master-apprentice contract actually enforced? Historians have found that a substantial number of contracts were not completed (De Munck and Soly, 2007 p. 10). Wallis (2008, pp. 839-40) has shown that in late seventeenth century London a substantial number of apprentices left their original master before completing the seven mandated years of their apprenticeship. The main reason was that the rigid seven year duration stipulated by the 1562 Statute of Artificers (which regulated apprenticeship) was rarely enforced, as were most other stipulations contained in that law (Dunlop, 1911, 1912).[9] As Wallis (2008, p. 854) remarks, "like many other areas of premodern regulation, the tidy hierarchy of the seven-year apprenticeship leading to mastery was more ideal than reality." Rather than an indication of contractual failure, the large number of apprentices that did not "complete" their terms indicates a greater flexibility in Britain. Moreover, many of them quit during their terms, and given the relatively small number of lawsuits filed against such apprentices (Rushton 1991, p. 94) it seems that many of the early departures were by mutual consent (see also Wallis 2008, p. 844).

The flexibility of the contracts in pre-Industrial Revolution England limited the risk each contracting party faced from the opportunistic behavior of the other. This institution, then, would be more successful in terms of transmitting existing skills between generations in an efficient manner. Once an apprentice had mastered a skill, there would be little point in staying on. Moreover, in many documented cases apprentices were "turned over" to another master—by some calculation this was true of 22 percent of all apprentices who did not complete their term (Wallis, 2008, pp. 842-43). There could be many reasons for this, of course, including the master falling sick or being otherwise indisposed. But also, at least some apprentices might have found that their master did not teach them best practice techniques or that the trade they were learning was not as remunerative as some other.

---

[9]For a more nuanced view, see Davies 1956, who argues that enforcement was a function of the economic circumstances, but agrees that there is little evidence of apprentices being sued or denied the right to exercise their occupation for having served fewer than seven years.

The exact mechanics of the skill transmission process are hard to nail down. After all, the knowledge being taught was tacit, and mostly consisted of imitation and learning-by-doing. It surely differed a great deal from occupation to occupation. Moreover, our own knowledge is biased to some extent by the better availability of more recent sources. All the same, Steffens (2001) has suggested that much of the learning occurred through apprentices "stealing with their eyes" (p. 131) – meaning that they learned mostly through observation, imitation, and experimentation. The tasks to which apprentices were put at first, insofar that they can be documented at all, seem to have consisted of rather menial assignments such as making deliveries, cleaning and guarding the shop. Only at a later stage would an apprentice be trusted with more sensitive tasks involving valued customers and expensive raw materials (Lane, 1996, p. 77). Yet they spent most of their waking hours in the presence of the master and possibly more experienced apprentices and journeymen, and as they aged they gradually would be trusted with more advanced tasks.[10]

One of the most interesting findings of the new research on apprenticeship, which is central to the theory developed below, is that in Europe family ties were relatively less important than elsewhere in the world, such as India (Roy, 2013, pp. 71, 77). In China, guilds existed, but were organized along clan lines and it is within those boundaries that apprenticeship took place (Moll-Murata, 2013, p. 234). In contrast, Europeans came to organize themselves along professional lines without the dependence on kinship (Lucassen, de Moor, and van Zanden, 2008, p. 16). Comparing China and Europe, van Zanden and Prak (2013a) write: "In China, training was provided by relatives, and hence a narrow group of experts, instead of the much wider training opportunities provided by many European guilds." The contrast between Asia and Europe in systems of knowledge transmission is also emphasized by van Zanden (2009): "We can distinguish two different ways to organize such training: in large parts of the world the family or the clan played a central role, and skills were transferred from fathers to sons or other members of the (extended) family. In fact, in parts of Asia, being a craftsman was largely hereditary .... In contrast to the relatively closed systems in which the family played a central role, Western Europe had a formal system of apprenticeship—organized by guilds or similar institutions—and in principle open to all." In Western Europe, despite the fact

---

[10]Wallis (2008, p. 849) compares the process with what happens in more modern days amongst minaret builder apprentices in Yemen: "instruction is implicit and fragmented, questions are rarely posed, and reprimands rather than corrections form the majority of feedback." De Munck makes a similar point when he writes that "masters were merely expected to point out what had gone wrong and what might be improved" (cited in De Munck and Soly 2007, p. 16 and p. 79).

that within the guilds the sons of masters received preferential treatment and that train-ing with a relative resolved to a large extent the contractual problems, following in the footsteps of the parents gradually fell out of favor (Epstein and Prak 2008, p. 10). The examples of Johann Sebastian Bach and Leopold Mozart notwithstanding, fewer and fewer boys were trained by their fathers. By the seventeenth century, apprentices who were trained by relatives were a distinct minority, estimated in London to be somewhere between 7 and 28 percent (Leunig, Minns, and Wallis 2011, p. 42). Prak (2013, p. 153) has calculated that in the bricklaying industry, fewer than ten percent continued their fathers' trades. This may have been a decisive factor in the evolution of apprenticeship as a market phenomenon in Europe, but not elsewhere.[11]

2.3   Mobility and the Diffusion of Knowledge

In premodern Europe, as early as fifteenth century Flanders, artisans were mobile. In England, such mobility was particularly pronounced (Leunig, Minns, and Wallis 2011), with lads from all over Britain seeking to apprentice in London, not least of all the young James Watt and Joseph Whitworth, two heroes of the Industrial Revolution. But as Sta-bel (2007, p. 159) notes, towns and their guilds had to accept and acknowledge skills acquired elsewhere, even if they insisted that newcomers adapt to local economic stan-dards set by the guilds. Constraints were more pronounced on the continent, but even here apprentices came to urban centers from smaller towns or rural regions (De Munck and Soly, 2007, p. 17), and mobility of artisans and the skills they carried with them extended to all of Europe.

The idea of the "journeyman" or "traveling companion" was that after completing their training, new artisans would travel to another city to acquire additional skills before they would qualify as masters—much like postdoctoral students today (Lis, Soly, and Mitzman 1994, Robert 1979). As such, journeymanship was traditionally the "inter-mediate stage" between completing an apprenticeship and starting off as a fullfledged master. Journeymen and apprentices are known to have traveled extensively as early as the fourteenth century, often on a seasonal basis, a practice known as "tramping." By the early modern period, this practice was fully institutionalized in Central Europe (Epstein, 2013, p. 59). Itinerant journeymen, Epstein argues, learned a variety of tech-niques practiced in different regions and were instrumental in spreading best-practice

---

[11]The cases of Japan and the Ottoman Empire are less clear cut; guilds clearly played some role here (see Nagata 2007, 2008, Yildirim 2008), but less is known about their role for organizing apprenticeship and the importance of family ties in the selection of apprentices.

techniques. Towns that believed to enjoy technological superiority forbade the practice of tramping and made apprentices swear not to practice their trades anywhere else, as with Nuremberg metal workers and Venetian glassmakers (ibid., pp. 60-61). Such prohibitions were ineffective at best and counterproductive at worst.

Not every apprentice had to go through journeymanship, and relatively little is known about how long it lasted and how it was contracted for. Journeymen have been regarded by much of the literature as employees of masters, and were often organized in *compagnonnages* which frequently clashed with employers. Journeymen in many cases were highly skilled workers, but more mobile than masters. Known as "travellers" or "tramps," they often chose to bypass the formal status of master but prided themselves on their skills, considering themselves "equal partners" to masters (Lis, Soly, and Mitzman 1994, p. 19). Their mobility lent itself to the creation of networks in the same lines of work, and it stands to reason that technical information flowed fairly freely along those channels of communication. But skilled masters, too, traveled across Europe, often deliberately attracted by mercantilist states or local governments keen to promote their manufacturing industries through the recruitment of high-quality artisans. Technology diffusion occurred largely through the migration of skilled workers, or through apprentices traveling to learn from the most renowned masters (and then returning home). Interestingly, such migration seems to have focused mostly on towns in which the industry already existed and which were ready to upgrade their production techniques (Belfanti 2004, p. 581).

2.4 Apprenticeship and Guilds

There has been a lively debate in the past two decades about the role of the guilds in premodern European economies. Traditionally relegated by an earlier literature to be a set of conservative, rent-seeking clubs, a revisionist literature has tried to rehabilitate craft guilds as agents of progress and technological innovation. Part of that storyline has been that guilds were instrumental in the smooth functioning of apprenticeships. As noted, given the potential for market failure due to incomplete contracts, incentive incompatibility, and poor information, agreements on intergenerational transmission of skills needed enforcement, regulation, and supervision. In a setting of weak political systems, the guilds stepped in and created a governance system that was functional and productive (Epstein and Prak 2008; Lucassen, de Moor, and van Zanden 2008; van Zanden and Prak 2013b). In a posthumously published essay, Epstein stated that the

details of the apprenticeship contract had to be enforced through the craft guilds, which "overcame the externalities in human capital formation" by punishing both masters and apprentices who violated their contracts (Epstein 2013, pp. 31-32). The argument has been criticized by Ogilvie (2014, 2016). Others, too, have found cases in which the nexus between guilds and apprenticeships proposed by Epstein and his followers does not quite hold up (Davids, 2003, 2007).

The reality is that some studies support Epstein's view to some extent, and others do not. The heated polemics have made the more committed advocates of both positions state their arguments in more extreme terms than they can defend. Guilds were institutions that existed through many centuries, in hundreds of towns, and for many occupations. This three-dimensional matrix had a huge number of elements, and it stands to reason that things differed over time, place, and occupation.

Most scholars find themselves somewhere in between. Guilds were at times hostile to innovation, especially in the seventeenth and eighteenth centuries, and under the pretext of protecting quality they collected exclusionary rents by longer apprenticeships and limited membership. But in some cases, such as the Venetian glass and silk industries, guilds encouraged innovation (Belfanti 2004, p. 576). Their attitude to training, similarly, differed a great deal over space and time. Davids (2013, p. 217), for instance, finds that in the Netherlands "guilds normally did not intervene in the conditions, registration, or supervision of [apprenticeship] contracts." Unger (2013, p. 203), after a meticulous survey, must conclude that the "precise role of guilds in the long term evolution of shipbuilding technology remains unclear." Moll-Murata (2013, p. 256), in comparing the porcelain industries in the Netherlands and China, retreats to a position that "contrasting the guild rehabilitationist [Epstein's] and the guild-critical positions is difficult to defend . . . we find arguments supporting both propositions."

Guilds and apprenticeship overlapped, but they did not strictly require each other, especially not after 1600. Apprenticeship contracts could find alternative enforcement mechanisms to guilds. In the Netherlands local organizations named *neringen* were established by local government to regulate and supervise certain industries independently of the guilds. They set many of the terms of the apprenticeship contract, often the length of contract and other details (Davids, 2007, p. 71). Even more strikingly, in Britain, most guilds gradually declined after 1600 and exercised little control over training procedures (Berlin, 2008). Moreover, informal institutions and reputation mechanisms in many places helped make apprenticeship work even in the absence of guilds. As Humphries

(2003) argues, apprenticeship contracts in England may have been, to a large extent, self-enforcing in that opportunistic behavior in fairly well-integrated local societies would be punished severely by an erosion of reputation. Market relationships were linked to social relationships, and such linkages are a strong incentive toward cooperative behavior (Spagnolo 1999). For example, a master found to treat apprentices badly might not only lose future apprentices, but also damage relations with his customers and suppliers. The same was true for the apprentices, whose future careers would be damaged if they were known to have reneged on contracts. If both master and apprentice expected this in advance, in equilibrium they would not engage in opportunistic behavior and would try to make their relationship as harmonious as possible. The limits to such self-enforcing contracts are obvious. Mobility of apprentices after training would mean that the the reach of reputation was limited, and in larger communities the reputation mechanism would be ineffective. Substantial opportunistic behavior could cause the cooperative equilibrium to unravel.

All the same, it has been stressed that despite the convincing evidence that guilds in some cases helped in the formation of human capital and supported innovation, the two economies in which technological progress was the fastest after 1600 were the Netherlands and Britain, the two countries in which guilds were relatively weak (Ogilvie, 2016). That such a correlation does not establish causation goes without saying, but it does serve to warn us against embracing the revisionist view of guilds too rashly.

In the theory articulated below, the growth implications of the guild system can be assessed according to their next best alternative. If the state is sufficiently strong to enforce contracts and enable apprenticeship without guilds being involved, the anticompetitive aspect of guilds dominates, and thus guilds hinder growth (consistent with faster growth in the Netherlands and Britain after 1600, when the state increasingly took over functions once served by guilds and cities). But when the state is weak, and the choice is between apprenticeship provided via guilds or via clans, the faster dissemination of knowledge associated with guilds dominates. We now turn to the theory that spells out these results in a formal model of knowledge transmission.

3   A Model of Pre-industrial Knowledge Growth

In this section, we develop an explicit model of knowledge creation and transmission in a pre-industrial setting. By pre-industrial, we mean that aggregate production relies on a land-based technology that exhibits decreasing returns to the size of the population.

In addition, there is a positive feedback from income per capita to population growth, implying that the economy is subject to Malthusian constraints. Compared to existing Malthusian models, the main novelty here is that we explicitly model the transmission of knowledge from generation to generation and the resulting technological progress. This allows us to to analyze how institutions affect the transmission of knowledge, and how this interacts with the usual forces present in a Malthusian economy.

3.1 Preferences, Production, and the Productivity of Craftsmen

The model economy is populated by overlapping generations of people who live two periods, childhood and adulthood. All decisions are made by adults, whose preferences are given by the utility function:

$$u(c, I') = c + \gamma I', \tag{1}$$

where c is the adult's consumption and I' is the total future labor income of this adult's children. The parameter $\gamma > 0$ captures altruism towards children. The role of altruism is to motivate parents' investment in their children's knowledge.

The adults work as craftsmen in a variety of trades. At the beginning of a period, the aggregate economy is characterized by two state variables: the number of craftsmen N, and the amount of knowledge k in the economy. Craftsmen are heterogeneous in productivity, and knowledge k determines the average productivity of craftsmen in a way that we make precise below. We start by describing how aggregate output in our economy depends on the state variables N and k.

The single consumption good (which we interpret as a composite of food and manufactured goods) is produced with a Cobb-Douglas production function with constant return to scale that uses land X and effective craftsmen's labor L as inputs:

$$Y = L^{1-\alpha} X^{\alpha}, \tag{2}$$

with $\alpha \in (0, 1)$. The total amount of land is normalized to one, $X = 1$. Land is owned by craftsmen.[12]

---

[12]Our main results would be identical if a separate class of landowners were introduced. The model abstracts from an explicit farming sector; however, it would be straightforward to include farm labor as an additional factor of production (see Appendix A), or alternatively we can interpret some of the adults who we refer to as craftsmen as farmers.

The effective labor supply by craftsmen L is a CES aggregate of effective labor supplied in different trades j:

$$L = \left(\int_0^1 (L_j)^{\frac{1}{\lambda}} dj \right)^{\lambda}, \tag{3}$$

with $\lambda > 1$. The elasticity of substitution between the different trades is $\lambda/(\lambda - 1)$. The distinction among different trades of craftsmen (watchmaker, wheelwright, blacksmith etc.) is important for our analysis of guilds below, which we model as coalitions of the craftsmen in a given trade. However, the equilibrium supply of effective labor will turn out to be the same in all trades, so that $L_j = L$ for all j. For most of our analysis, we can therefore suppress the distinction between trades from the notation.

We now relate the supply of effective labor by craftsmen L in efficiency units to the number of craftsmen N and the state of knowledge k. Craftsmen are heterogenous in knowledge. The productive knowledge of a craftsman i is measured by a cost parameter h_i, where a lower h_i implies that the master can produce at lower cost and hence has more productive knowledge. Intuitively, different craftsmen may apply different methods and techniques in their production, which vary in productivity. Specifically, the output q_i of a craftsman with knowledge h_i is given by:

$$q_i = h_i^{-\theta}. \tag{4}$$

The final-goods technology (2) is operated by a competitive industry. Given the Cobb-Douglas production function, this implies that craftsmen receive share $1 - \alpha$ of total output as compensation for their labor, and consequently the labor income of a craftsman supplying q_i efficiency units of craftsmen's labor is:

$$I_i = q_i (1 - \alpha) \frac{Y}{L}. \tag{5}$$

The heterogeneity in the cost parameter h_i among craftsmen takes the specific form of an exponential distribution with distribution parameter k:

$$h_i \sim \text{Exp}(k).$$

Given the exponential distribution, the expectation of h_i is given by $\mathbb{E}[h_i] = k^{-1}$. Hence, higher knowledge k corresponds to a lower average cost h_i and therefore higher productivity. We assume that the same k applies to all trades. Given the exponential distri-

bution for h_i and (4), output q_i follows a Fréchet distribution with shape parameter $1/k$ and scale parameter $1/\theta$.

We can now express the total supply of effective labor by craftsmen as a function of state variables. The average output across craftsmen is given by:

$$q = \mathbb{E}\,(q_i) = \int_0^\infty h_i^{-\theta}\,(k\exp(-kh_i))\,dh_i = k^\theta\Gamma(1-\theta), \tag{6}$$

where $\Gamma(t) = \int_0^\infty x^{t-1}\exp(-x)dx$ is the Euler gamma function. The total supply of effective craftsmen's labor L is then given by the expected output per craftsman $\mathbb{E}\,(q_i)$ multiplied by the number of craftsmen N:

$$L = N\,k^\theta\,\Gamma(1-\theta). \tag{7}$$

Income per capita can be computed from (2) and (7) as:

$$y = \frac{Y}{N} = \frac{L^{1-\alpha}}{N} = \Gamma(1-\theta)^{1-\alpha}\,k^{(1-\alpha)\theta}\,N^{-\alpha}. \tag{8}$$

3.2 Population Growth and the Malthusian Constraint

So far, we have described how total output (and hence output per adult) depends on the aggregate state variables N and k. Next, we specify how these state variables evolve over time. We start with population growth. Consistent with evidence from pre-industrial economies (see Ashraf and Galor 2011), the model allows for Malthusian dynamics.[13] The presence of land in the aggregate production function implies decreasing returns for the remaining factor L, which gives rise to a Malthusian tradeoff between the size of the population and income per capita. The second ingredient for generating Malthusian dynamics is a positive feedback from income per capita to population growth. While often this relationship is modeled through optimal fertility choice,[14] we opt for a simpler mechanism of an aggregate feedback from income per capita to mortality rates. Every

---

[13]Empirical work has found both a fertility and a mortality link to income per capita in medieval England, but gradually weakening over time (Kelly and Ó Gráda 2012 and 2014). The "fundamentalist" Malthusian assumption that all productivity gains eventually are translated into population growth so that the "iron law" holds fully is made here for simplification; our results for institutional comparisons would be similar in a framework that allows for growing income per capita even in the long term.

[14]Fertility preferences can be motivated through parental altruism (Barro and Becker 1989 and applied in a Malthusian context by Doepke 2004, among others) or through direct preferences over the quantity and quality of children (e.g., Galor and Weil 2000 and de la Croix and Doepke 2003).

adult gives birth to a fixed number $\bar{n} > 1$ of children. The fraction of children that survives to adulthood depends on aggregate output per adult y, namely:

$$n = \bar{n} \min [1, s\,y]. \tag{9}$$

Here $\min[1, s\,y]$ is the fraction of surviving children, and n is the number of surviving children per adult. This function captures that low living standards (e.g., malnutrition) make people (and in particular children) more susceptible to transmitted diseases, so that low income per capita is associated with more frequent deadly epidemics. In recent times, we can also envision s to depend on medical technology (i.e., the invention of antibiotics would raise s). However, given that we analyze preindustrial growth, we will assume that s is fixed. We will also focus attention on a phase of development where the mortality tradeoff is still operative, so that survival is less than certain and $n = \bar{n}s\,y$. The law of motion for population then is:

$$N' = n\,N = \bar{n}\,s\,y\,N = \bar{n}\,s\,Y.$$

Consider a balanced growth path in which the stock of knowledge k grows according to a constant growth factor g:

$$g = \frac{k'}{k}.$$

In such a balanced growth path, the Malthusian features of the model economy impose a relationship between growth in knowledge g and population growth n, as shown in Proposition 1.

Proposition 1 (The Malthusian Constraint).
 Along a balanced growth path, the growth factor of technology g and the growth factor of population n satisfy:

$$g^{\theta(1-\alpha)} = n^{\alpha}. \tag{10}$$

Proof. Income per capita y is given by (8). Along a balanced growth path, y is constant, and hence (10) has to hold in order to keep the right-hand side of (8) constant, too. ∎

The Malthusian constraint states that faster technological progress is linked to higher population growth. Given (10), a faster rate of technological progress is also associated with a higher level of income per capita. Income per capita is constant in any

balanced growth path: Malthusian dynamics rule out sustained growth in living standards, because accelerating population growth ultimately would overwhelm productivity growth. Instead, economies with faster accumulation of knowledge will be characterized by faster population growth and hence, over time, increasing population density.

3.3   Apprenticeship, Innovation, and the Evolution of Knowledge

We now turn to the accumulation of knowledge in our model economy. In a given period, all productive knowledge is embodied in the adult workers. During childhood, people have to acquire the productive knowledge of the previous generation. There are two sources of increasing knowledge across generations. First, craftsmen are heterogeneous in their productive knowledge. Young craftsmen can learn from multiple adult craftsmen, and then apply the best of what they have learned. This knowledge dissemination process results in endogenous technological progress. In addition, after having acquired knowledge from the elders, young craftsmen can innovate, i.e., generate an idea that may improve on what they have learned, resulting in a second source of technological progress.

In order to model the idea that apprentices (or their parents) are subject to imperfect information on the efficiency of the different masters, we assume that the young can observe the efficiency of masters only by working with them as apprentices. Consider an apprentice who learns from m masters indexed from 1 to m (the choice of m will be discussed below). The efficiency h_L learned during the apprenticeship process is:

$$h_L(m) = \min \{h_1, h_2, \ldots, h_m\}. \tag{11}$$

Hence, apprentices acquire the cost parameter of the most efficient (i.e., lowest cost) master they have learned from. After learning from masters, craftsmen attempt to innovate by generating a new idea characterized by cost parameter h_N. The quality of the idea is random, and it may be better or worse than what they already know. As adult craftsmen, they use the highest efficiency they have attained either through learning from elders or through innovation, so that the final cost parameter h' is given by:

$$h' = \min \{h_L, h_N\}. \tag{12}$$

As will become clear below, the model can generate sustained growth even if the rate of innovation is zero (i.e., own ideas are always inferior to acquired knowledge). In

that case, the dissemination process of existing ideas is solely responsible for growth. However, allowing for innovation allows for a positive rate of productivity growth even if each child learns only from a single master.

Recall that the distribution of the h_i among adult craftsmen is exponential with distribution parameter k. The distribution of new ideas is also exponential, and the quality of new ideas depends on existing average knowledge:

$$h_N \sim \text{Exp}(\nu k).$$

That is, the more craftsmen already know, the better the quality of the new ideas generated. The parameter ν measures relative importance of transmitted knowledge and new ideas. If ν is close to zero, most craftsmen rely on existing knowledge, and if ν is large, innovation rather than the dissemination of existing ideas through apprenticeship is the key driver of knowledge.

The exponential distributions for ideas imply that, given the knowledge accumulation process described by (11) and (12), the knowledge distribution preserves its shape over time (as in Lucas 2009). Specifically, if each young craftsman learns from m masters that are drawn at random we have:[15]

$$h_L = \min\{h_1, h_2, \ldots, h_m\} \sim \text{Exp}(mk),$$
$$h' = \min\{h_L, h_N\} \sim \text{Exp}(mk + \nu k).$$

Hence, with m randomly chosen masters per apprentice, aggregate knowledge k evolves according to:

$$k' = (m + \nu)k. \tag{13}$$

The market for apprenticeship interacts with population growth. In particular, if each master takes on a apprentices, and each apprentice learns from m masters, the condition for matching demand and supply of apprenticeships is:

$$N'm = Na. \tag{14}$$

---

[15]This result follows from the min stability property of the exponential distribution. In particular, if h_a and h_b are independent exponentially distributed random variables with rates k_a and k_b, then $\min[h_a, h_b]$ is exponentially distributed with rate $k_a + k_b$.

We ignore integer constraints and treat m and a as continuous variables. Below, we will focus on equilibria where each apprentice chooses the same number of masters m, and each master has the same number of apprentices a.

We now arrive at the core of our analysis, namely the question of how the number and identity of masters for each apprentice are determined. Apprenticeship is associated with costs and benefits. While working as an apprentice with a master, each apprentice produces $\kappa > 0$ units of the consumption good (this is in addition to the output generated by the aggregate production function). This output is controlled by the master. In turn, a master who teaches a apprentices incurs a utility cost $\delta(a)$, where $\delta(0) = 0$, $\delta'(a) > 0$, and $\delta''(a) > 0$ (i.e., the cost is increasing and convex in a). Incurring this cost is necessary for transmitting knowledge to the apprentices. We assume for simplicity that the function $\delta(\cdot)$ is quadratic, i.e. $\delta(a) = \frac{\bar{\delta}}{2}a^2$.

If a master takes on a apprentices but then puts no effort into teaching, the apprentices still generate output κa by assisting the master in production. Thus, there is a moral hazard problem: Masters may be tempted to take on apprentices, appropriate production κa, but not actually teach, saving the cost $\delta(a)$.

Dealing with this moral hazard problem is a key challenge for an effective system of knowledge transmission. The danger of moral hazard is especially severe here because the very nature of apprenticeship defines it as the quintessential incomplete contract (see Section 2). In a modern market economy, we envision that such problems are dealt with by a centralized system of contract enforcement. In such a system, a parent would write contracts with masters to take on the children as apprentices. A price would be agreed on that is mutually agreeable given the cost of training apprentices and the parent's desire, given altruistic preferences (1), to provide the children with future income. Courts would ensure that both parties hold up their end of the bargain.

In pre-industrial societies lacking an effective system of contract enforcement, other institutions would have to ensure an effective transmission of knowledge from the elders to the young. Our view is that variation in these alternative institutions across countries and world regions plays a central role in shaping economic success and failure in the pre-industrial era. After a brief discussion of model assumptions, we analyze specific, historically relevant institutions in the context of our model of knowledge-driven growth.

3.4 Discussion of Model Assumptions

Our model of growth in the pre-industrial economy is stylized and relies on a set of specific assumptions that yield a tractable analysis. We conclude our description of the model with a discussion of the role and plausibility of the assumptions that are most central to our overall argument.

Most importantly, apprenticeship institutions matter in our economy because the knowledge of masters is not publicly observable. This creates the incentive for apprentices to sample the knowledge of multiple masters to gain productive knowledge, and implies that institutions that determine how apprentices are matched to masters matter for growth. To maintain tractability, in the model the lack of information on productivity is severe: Nothing at all is known about the productivity of different masters, even though there is wide variation in their actual productivity. Taken at face value, this assumption is clearly implausible. However, possible concerns about its role can be addressed in two ways.

First, in our model all knowledge differences between masters are actual productivity differences, i.e., masters who know more produce more. A realistic alternative possibility is that at least some variation in knowledge is in terms of "latent" productivity, i.e., some masters may know techniques and methods that will turn out to be highly productive and important at a later time when combined with other knowledge, but do not give a productivity advantage in the present. A well known example are the inventions of Leonardo da Vinci which could not be implemented given the knowledge of his age, but which turned into productive knowledge centuries later. Similarly, the success of the steam engine was based in large part on a set of gradual improvements in craftmen's ability to work metal to precise specifications; for instance, steam engines work only if the piston can move easily in the cylinder but with a tight fit. Many improvements in techniques would have been of comparatively little value when first invented, but then became critical later on. Along these lines, in Appendix B we describe an extension of our model where a craftsman's output can be constrained by the state of aggregate knowledge. This version leads to exactly the same implications as the simpler setup described here, but actual variation in productivity is much smaller than variation in latent productivity, so that imperfect information on underlying productivity appears more plausible.

Second, it would be possible to relax the assumption of total lack of information about productivity, and instead assume that an informative, but imperfect, signal of each mas-

ter's productivity was available.[16] In such a setting, more productive masters could command higher prices for apprenticeships, they would employ a larger number of apprentices, and the spread of productive knowledge would be faster. As we document in Section 2, the historical evidence for Europe suggests that, indeed, more productive and knowledgeable masters were able to command higher prices and attract more apprentices. However, as long as information on productivity is less than perfect, the basic tradeoffs articulated by our analysis and the comparative growth implications of the institutions analyzed below would be the same. Less-than-perfect information about productivity is highly plausible; even in today's world of instant communication and online discussion boards, for example, graduate students do not have perfect information about which advisor will be the best match for them. We adopt the extreme case of complete lack of observability for tractability; without this assumption the distribution of knowledge would not preserve its shape over time, so that we would have to rely on numerical simulation for all results.[17]

In addition, the master-apprentice relationship in the model is simplified compared to reality. We use a setting with one-sided moral hazard, i.e., masters can cheat apprentices, but not vice versa. In reality, moral hazard was a major concern on both sides of the master-apprentice relationship. This assumption is introduced merely to simplify the analysis. It would be straightforward to introduce two-sided moral hazard in our setting, and the role of institutions for mitigating moral hazard would be unchanged.

Finally, in the model apprentices interact in the same way with all masters they learn from, and they make a one-time choice of the number of masters to learn from. As ever, reality is substantially more complicated; choices of whom to learn from unfolded sequentially over time, and apprentices generally did only one full apprenticeship, followed by other shorter interactions during journeymanship. Once again, these assumptions are for simplicity and tractability, but are not central to our main results regarding the role of institutions for knowledge transmission. The key point in the theoretical setup is that apprentices are able to observe the efficiency of multiple masters and adopt the techniques of the most efficient master. It is not necessary that apprentices spend

---

[16]See Jovanovic (2014) for a study where a signal of skill is available, and assortative matching of young and old workers is an important driver of growth.

[17]Luttmer (2015) provides an alternative approach for modeling the assignment of students to teachers. Luttmer's model has the advantage of allowing for observability and not relying on an unbounded support of existing knowledge, albeit at the cost of a considerably more complex analysis.

equal time with each master; in reality, an interaction may be brief and end once an apprentice ascertains that a given master has nothing new to offer. The model abstracts from such differentiated interactions and imposes symmetrical master-apprentice relations to improve tractability. Having said that, when matching the model to data, care should be taken to account for the fact that "apprenticeships" in the model correspond to a wider range of interactions in reality.

4 Comparing Institutions for Knowledge Transmission

The crucial question in our theory is how the moral hazard problem inherent in apprenticeship is resolved. If masters do not make an effort to teach their apprentices, parents will have no incentive to send children to learn from masters outside the family. Apprentices would not learn anything, whereas masters would gain the apprentices' production κ. Parents would be better off keeping children at home, thereby keeping output κ in the family. Thus, for apprenticeship outside the immediate family to be feasible (and thus for knowledge to disseminate), an enforcement mechanism is required in order to provide incentives for masters to exert effort.

4.1 Centralized versus Decentralized Institutions

We consider two types of institutions, characterized by centralized versus decentralized enforcement. Under centralized enforcement, people can write contracts specifying that the master must put in effort (and indicating the price of apprenticeship), and there is a centralized system (such as courts) that punishes anyone who breaks a contract. In contrast, in a decentralized system no such central authority exists, and instead people have to form coalitions to maintain a sufficient threat of punishment to resolve the moral hazard problem.[18]

To allow for the possibility of decentralized enforcement, we assume that each adult can inflict a utility cost (damage) on any other adult.[19] However, the punishment that a single adult can mete out is not sufficient to induce a master to put in effort, i.e., the punishment is lower than the cost of training a single apprentice. In contrast, coalitions

---

[18]We should note that in reality, the distinction between centralized and decentralized institutions is less sharp than in our theory. Even where centralized enforcement institutions existed, they were often complemented by a self-enforcing mechanism based on trust and reputation (Humphries 2003; Mokyr 2008).

[19]The cost can be interpreted as physical punishment, as destruction of property, or as spreading rumors that induce others not to buy from the individual in question.

of people can always make threats that are sufficient to guarantee compliance. An effective threat of punishment therefore requires coordination among parents. Coordination, in turn, requires communication: For a master's shirking to have consequences, the fact of the shirking has to be communicated to all would-be punishers. Thus, the extent to which people are able to communicate with each other partly determines how much knowledge transmission is possible.

Over time, societies have differed in the extent and manner in which individuals were connected in communication networks. We consider two different scenarios for decentralized enforcement, the "family" and the "clan," which we consider particularly relevant for contrasting Europe during the Early Middle Ages with China, India, and the Middle East during the same period and beyond.

The decentralized systems correspond to a period when centralized enforcement was not yet sufficiently effective. Even if courts existed, contract enforcement was often costly, slow, and uncertain. More importantly, for centuries the reach of the state and hence its courts was severely limited. Europe, for example, used to consist of hundreds of independent sovereign entities, and the enforcement of the law outside one's immediate surroundings (say, the city of residence) was weak. With this in mind, the first centralized enforcement institution that we consider is organized not by the state but by a coalition of all the masters in a given trade: a "guild." The guild monitors the behavior of its members and enforces the apprenticeship contracts between parents and masters. However, the guild also has anti-competitive features. It can set the price of apprenticeship, thereby exploiting its monopoly in a given trade. Guilds played a central role in European economic life during the Middle Ages, and our theory will allow us to assess their implications for knowledge creation and dissemination.

The final institution that we consider is the "market," where there is a centralized enforcement system for all trades as in a modern market economy. Importantly, under this institution the government not only enforces contracts, but also prevents collusion; trades are no longer allowed to form guilds that limit entry and lower competition, and both parents and masters act as price takers. The market institution corresponds to the final stages of the pre-industrial economy, when in Europe nation states became powerful and increasingly abolished the traditional privileges of guilds.

4.2 The Family

Decentralized institutions enforce apprenticeship agreements through the formation of coalitions of parents that coordinate on a sufficient threat of punishment for shirking masters. Different decentralized institutions are distinguished by the size of these coalitions and the identity of their members. For the formation of a coalition to be feasible, the members have to be able to communicate with each other about the behavior of masters. Hence, one polar case is where members of different families are unable to communicate with each other, so that no coalitions can be formed. The lack of communication rules out coordinating on punishing shirking masters. As a consequence, apprenticeship outside the immediate family is impossible, i.e., each child learns only from the parent. In principle, the moral hazard problem is present even within the family. However, in utility (1) parents care about their own children, and we assume that the degree of altruism γ is sufficiently high for parents never to shirk when teaching their own children. The result is a "family equilibrium," i.e., an equilibrium where knowledge is transmitted only within dynasties, but there is no dissemination of knowledge across dynasties.

Formally, under decentralized institutions we model the knowledge accumulation decisions as a game between the craftsmen of a given generation. The strategy of a given craftsman has three elements:

1. Decide whether to send own children to others as apprentices for training, and if so, which compensation to pay the masters of one's children.
2. Decide whether to exploit one's own apprentices (if any).
3. Decide whom to punish (if anyone).

We focus on Nash equilibria.[20] The strategy profile for the family equilibrium is as follows:

- All craftsmen train their children on their own.
- If (off the equilibrium path) a master gets someone else's child as an apprentice, the master exploits the apprentice.
- No one ever punishes anyone.

---

[20]Given that there are subsequent generations, one could also define a dynamic game involving all generations. However, given that preferences are of the warm-glow type, decisions of future generations do not affect the payoffs of the current generation, so that dynamic considerations do not change the strategic tradeoffs faced by the players.

If communication outside the immediate family is impossible, the family equilibrium is the only equilibrium. The family equilibrium can also occur as a "bad" equilibrium in an economy where more communication links are available, but people fail to coordinate on a more efficient punishment equilibrium.[21]

Now consider the balanced growth path under the family equilibrium. We assume that the Malthusian feedback, parameterized by the maximum number of children $\bar{n}$ and the survival parameter s, is sufficiently strong for dynamics to lead to a balanced growth path in which income per capita is constant.[22] The following proposition summarizes the properties of the balanced growth path.

Proposition 2 (Balanced Growth Path in Family Equilibrium).
If altruism is sufficiently strong (i.e., γ is sufficiently large), there exists a unique balanced growth path under the family equilibrium with the following properties:

(a) *Each child trains only with his own parent: $m^F = 1$, and $a^F = n^F$.*
(b) *The growth factor g^F of knowledge k is:*

$$g^F = 1 + \nu.$$

(c) *The growth factor n^F of population N is:*

$$n^F = (1 + \nu)^{\frac{(1-\alpha)\theta}{\alpha}}.$$

(d) *Income per capita y^F is constant and satisfies:*

$$y^F = \frac{(1 + \nu)^{\frac{(1-\alpha)\theta}{\alpha}}}{\bar{n}\, s}.$$

Proof. See Appendix C. ∎

The condition for sufficient altruism reflects that parental altruism should be strong enough to overcome the disutility of teaching one's children. The rate of technological progress is positive in the family equilibrium, but small. This is because the only source of progress is the new ideas of craftsmen (recall that ν measures the quality of

---

[21]For any communication structure, the family equilibrium always exists, because in the expectation that no one else will punish shirking masters it is optimal to (i) never punish shirking masters either and (ii) not send one's own children to be apprenticed outside the family.
[22]The required assumptions can be made precise; what is key is that maximum population growth is larger than the maximum rate of effective productivity growth.

new ideas). New ideas are passed on to children, which makes children, on average, more productive than the parents. However, knowledge does not disseminate across dynasties. Given the growth rate of knowledge $g^F = 1 + \nu$, Malthusian dynamics ensure that population grows just fast enough to offset productivity growth and yield constant income per capita.
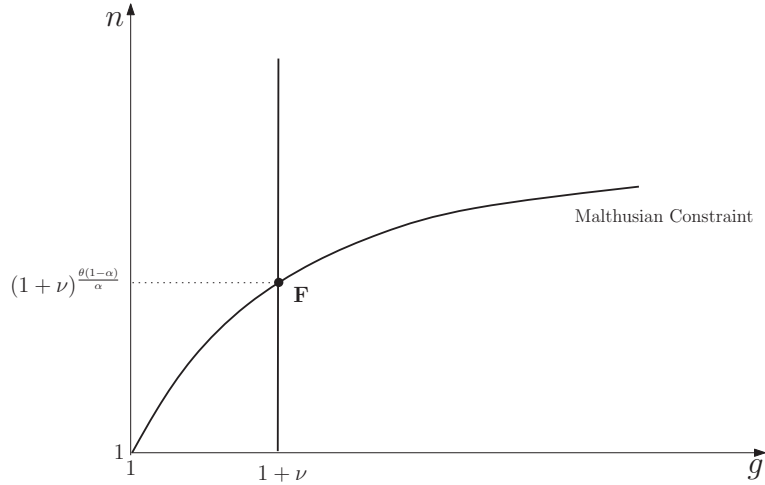

Figure 1: Productivity and Population Growth in the Family (**F**) Equilibrium

Figure 1 represents the determination of the balanced growth path in the family equilibrium. The concave curve represents the Malthusian constraint given by (10).[23] The intersection between this constraint and the line $g = 1 + \nu$ gives the balanced growth path under the family equilibrium **F**.

4.3 The Clan

Next, we consider economies where there is communication within an extended family or clan. While many other structures could be considered, the clan has particular historical significance because of its importance for organizing economic exchange in the major world regions outside Europe. Formally, we consider a setting where all members of a dynasty who share an ancestor o generations back can communicate (here $o = 0$ corresponds to the family equilibrium, $o = 1$ means siblings are connected, and so on). Now consider a potential "clan equilibrium" with the following equilibrium strategy profiles:

---

[23]The curve is concave if $\theta(1 - \alpha) < \alpha$, but results to do not depend on this condition.

- All craftsmen send their children to be trained by each master in the clan, and parents compensate masters for the apprenticeship by paying each $\delta'(a) - \kappa$ (the marginal cost), where a is the number of apprentices per master.
- All masters put effort into teaching.
- If (off the equilibrium path) a master cheats an apprentice, all current members of the clan punish the master.

For example, if $o = 1$, children are trained not only by their parents, but also by their aunts and uncles. For $o = 2$, second-degree relatives serve as masters, and so on.[24] Along a balanced growth path, the total number of adults (i.e., masters) belonging to the clan is $(n^c)^o$, where n^c is the rate of population growth in the balanced growth path. For learning from all current masters to be feasible, we assume that all members of the clan work in the same trade. An alternative setup allows for large clans that engage in many trades, in which case a child would be trained only by those masters in the clan who work in the child's chosen trade. In either case, we envision that in the clan equilibrium children obtain the knowledge of a handful of masters who belong to the same clan and to the same trade.

The following proposition summarizes the properties of the balanced growth path in the clan equilibrium.

Proposition 3 (Balanced Growth Path in Clan Equilibrium).
There is threshold $o_{\max} > 0$ such that if $o < o_{\max}$ and if altruism is sufficiently strong (i.e., γ is sufficiently large), there exists a balanced growth path in the clan equilibrium with the following properties:

(a) *The number of masters per child m is given by the number of adults in the clan, $m^c = (n^c)^o$, and the number of apprentices per master is $a^c = (n^c)^{o+1}$.*
(b) *The growth factor g_k^c of knowledge k is the solution to:*

$$g^c = 1 + \frac{\nu (n^c)^o}{g^c - \nu}. \tag{15}$$

---

[24] In reality, it may not be necessary to receive full training from all clan members. Instead, one could assume that apprentices initially search over the entire group, sample the masters' knowledge, but then spend most of their time learning from the clan member identified to have the lowest h. We adopt the simpler notion of learning equally from all masters to preserve the symmetry that makes the problem tractable.

(c) *The growth factor n_k^c of population N is given by:*

$$n^c = \left(g^c\right)^{\frac{(1-\alpha)\theta}{\alpha}}.$$

(d) *Income per capita is constant and satisfies:*

$$y^c = \frac{\left(g^c\right)^{\frac{(1-\alpha)\theta}{\alpha}}}{\bar{n}s}.$$

For $o = 0$, the balanced growth path coincides with the family equilibrium, whereas for $o > 0$ knowledge growth, population growth, and income per capita are higher compared to the family equilibrium. The growth g^c of knowledge k is increasing in the size of the clan o.

Proof. See Appendix D. ■

Parallel to the family equilibrium, the condition on sufficiently high altruism ensures that parents find it worthwhile to pay for the training of their children.[25] The upper bound $o_{\max}$ on the size of the clan limits productivity growth to a level where the Malthusian feedback is sufficiently strong to generate a balanced growth path with constant income per capita.

The clan equilibrium leads to a higher growth rate compared to the family equilibrium because children learn from more masters. In particular, they benefit not just from the new ideas of their own parent, but also from the new ideas of their aunts, uncles, and other current members of the clan. Thus, new knowledge disseminates more widely compared to the family equilibrium. However, there is still no dissemination of knowledge across clans. Equation (15) implies that as long as $v > 0$ (there is some innovation), a higher o (larger clans) leads to faster growth. However, if there are no new ideas, $v = 0$, the growth rate in the clan equilibrium is zero. Intuitively, in a clan the masters of a given apprentice all trained with the same masters when they were apprentices, which implies that they all started out with the same knowledge. If the masters don't

---

[25]Another possibility is that altruism is at a level sufficient for parents to want to send their children to some, but not all, available masters. Characterizing the balanced growth path in this case is more complicated, because the selection of which masters to train with is non-trivial. Nevertheless, the basic shortcoming of the clan-based institution, namely that different masters have similar knowledge and so less new knowledge can be gained by getting trained by more of them, would still apply in this type of equilibrium.

have new ideas of their own, studying with multiple masters does not provide any benefit over studying with only one of them. Hence, knowledge does not accumulate across generations.

Another way of stating this key point is that learning opportunities in the clan are limited, because the knowledge of the available masters is correlated. This correlation, in turn, arises from the fact that the available masters once learned from the same teachers, and hence acquired the same pooled knowledge present within the clan. As we will see, this issue of correlated knowledge across masters is the key distinction between the clan and institutions such as the guild and the market, which extend beyond blood relatives.
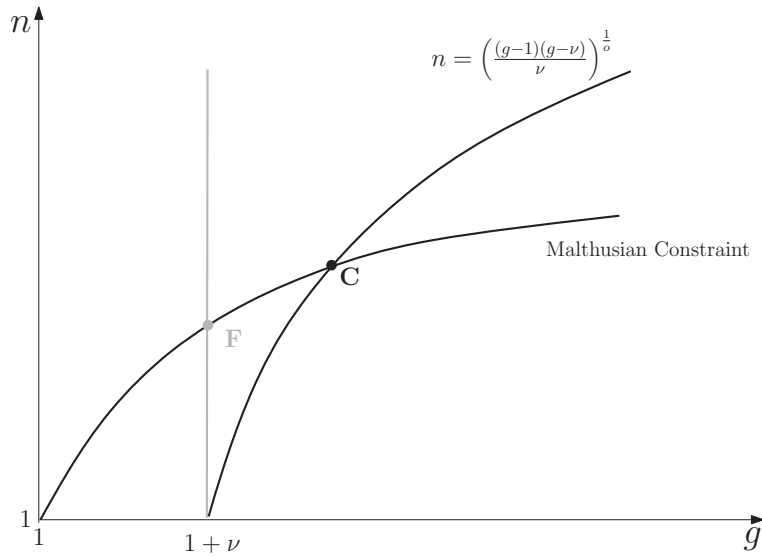

Figure 2: Productivity and Population Growth in the Clan (**C**) Equilibrium

Figure 2 represents the determination of the balanced growth path in the clan equilibrium. In addition to the Malthusian constraint (10), we have drawn the function

$$ n = \left(\frac{(g-1)(g-\nu)}{\nu} \right)^{\frac{1}{\sigma}}, \tag{16} $$

which is derived from (15). This function is equal to one when $g = 1 + \nu$, increases monotonically with g for $g > 1 + \nu$, and ultimately crosses the Malthusian constraint. The function (16) captures the relationship between population growth and the size of the clan. When $n = 1$, every person has one child, and hence there are no siblings and no aunts or uncles. Therefore, children can learn only from their own parent, who is the

31

sole adult member of the clan. At higher rates of population growth, the clan is bigger, and hence there are more masters who generate ideas and whom the young can learn from, resulting in faster technological progress.

4.4 The Market

At the opposite extreme (compared to the family) of enforcement institutions, we now consider outcomes in an economy with formal contract enforcement (as in the usual complete-markets model). All contracts are perfectly and costlessly enforced, so that masters who promise to train apprentices do not shirk. There is a competitive market for apprenticeship. Given market price p for training apprentices, masters decide how many apprentices to train, and parents decide how many masters to pay to train their children. In equilibrium, p adjusts to clear the apprenticeship market.

A craftsman's decision to take on apprentices is a straightforward profit maximization problem. In particular, given price p a master will choose the number of apprentices a to solve:

$$\max_a \left\{ p \, a + \kappa \, a - \delta(a) \right\}.$$

The benefit of taking on apprentices derives from the price p as well as the apprentices' production κ, and the cost is given by $\delta(a)$. Optimization implies that in equilibrium the price of apprenticeship equals the marginal cost of training an apprentice:

$$p = \delta'(a) - \kappa.$$

Now consider parents' choice of the number of masters m that their children should learn from. Given p, parents will choose m to maximize their utility (1):

$$\max_m \left\{ -p \, m \, n + \gamma \, \mathbb{E} \, I' \right\},$$

where n is the number of children and I' is the income of the child, which is given by (5). Each child's expected income depends on m, because learning from a larger number of masters increases the expected productivity (and hence income) of the child. The objective function is concave, because as m rises, the probability that an additional master will have higher productivity declines.

Lemma 1. *The first-order condition for the parent's problem implies:*

$$\delta'(a) - \kappa = \gamma \, \theta (1-\alpha) \frac{1}{m+v} \frac{Y'}{N'}. \tag{17}$$

Proof. See Appendix E. ∎

Notice that the decision problem implicitly assumes that the young apprentice gets m independent draws from the distribution of knowledge among the elders, as though the masters were drawn at random. The possibility of independent draws from the knowledge distribution is a key advantage of the market system over the clan system. In a clan, the potential masters have similar knowledge (because they learned from the same "grand" master), and hence the gain from studying with more of them is limited (there is still some gain because of the new ideas generated by masters). Of course, it would be even better to study only with masters known to have superior knowledge. We assume, however, that a master's knowledge can be assessed only by studying with them; hence, choosing masters at random is the best one can do.

The market equilibrium gives rise to a unique balanced growth path, which is characterized in the following proposition.

Proposition 4 (Balanced Growth Path in Market Equilibrium).
The unique balanced growth path in the market equilibrium has the following properties:

(a) *The number of apprentices per master* a^{M} *solves (17):*

$$\delta'(a^{\text{M}}) - \kappa = \gamma \, \theta (1-\alpha) \frac{1}{a^{\text{M}}/n^{\text{M}} + v} y^{\text{M}}, \tag{18}$$

and the number of masters per child m^{M} *is the solution to* $m^{\text{M}} = a^{\text{M}}/n^{\text{M}}$.

(b) *The growth factor* g^{M} *of knowledge k is given by:*

$$g^{\text{M}} = m^{\text{M}} + v.$$

(c) *The growth factor* n^{M} *of population N is given by:*

$$n^{\text{M}} = \left(g^{\text{M}}\right)^{\frac{(1-\alpha)\theta}{\alpha}}.$$

(d) Income per capita is constant and satisfies:

$$y^{\text{M}} = \frac{\left(g^{\text{M}}\right)^{\frac{(1-\alpha)\theta}{\alpha}}}{\bar{n}\,s}.$$

The market equilibrium yields higher growth in productivity and population and higher income per capita than does the clan equilibrium and the family equilibrium.

Proof. See Appendix F. ∎

To analyze the equilibrium, we can plug the expressions for a^{M}, m^{M}, and y^{M} into (17) to get:

$$\delta'((g^{\text{M}} - \nu)n^{\text{M}}) - \kappa = \gamma\theta(1-\alpha)\frac{1}{g^{\text{M}}}\,\frac{n^{\text{M}}}{\bar{n}\,s}. \tag{19}$$

This equation describes a relationship between g^{M} and n^{M} which we call the "apprenticeship market," as it is derived from demand for apprenticeship and the equilibrium condition on the apprenticeship market. Equation (19) can be rewritten as:

$$n^{\text{M}} = \frac{\kappa}{\bar{\delta}(g^{\text{M}} - \nu) - \dfrac{\gamma\theta(1-\alpha)}{\bar{n}\,s\,g^{\text{M}}}} \tag{20}$$

This function of g^{M} is plotted in Figure 3. The negative relationship between population growth and the rate of technical progress in (19) can be interpreted as follows. When fertility is higher, the market for apprenticeships is tighter, the equilibrium price of apprenticeship is higher, and parents demand fewer masters. Hence faster population growth is associated with lower productivity growth.

The market equilibrium leads to faster growth than the clan equilibrium does because knowledge is disseminated across ancestral boundaries throughout the entire economy. The masters teaching apprentices represent a wider range of knowledge, implying that more can be learned from them.[26] All of this is made possible by having a different enforcement technology for apprenticeship contracts, namely courts rather than punishment by clan members.

---

[26]The contrast between clan and market equilibrium is an example of social structure being important for economic outcomes; a similar application to technology diffusion is provided in the recent work by Fogli and Veldkamp (2012).
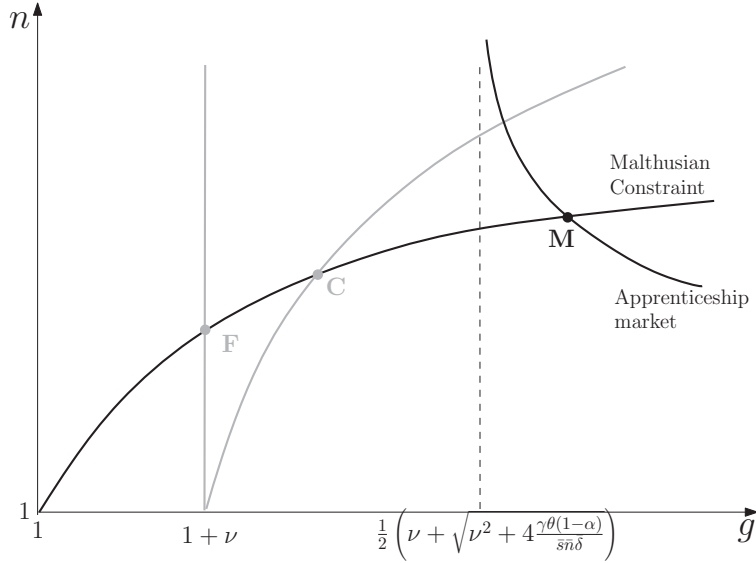
Figure 3: Productivity and Population Growth in the Market (**M**) Equilibrium

4.5 The Guild

Historically, economies did not transition directly from the family or clan equilibrium to the market equilibrium; rather, there were intermediate stages of semi-formal enforcement through institutions other than the state. In Europe, the key intermediate institution was the guild system, which for centuries regulated apprenticeship and knowledge transmission, at a time when state power was still weak. We now provide a formal characterization of a "guild equilibrium" as an intermediate step between the family equilibrium and the market equilibrium.

We envision a guild as an association of all masters involved in the same trade. In the production function (3), the effective labor supply from many different trades is combined with limited substitutability across trades, so that market power can arise. Allowing for heterogeneous labor supply by different trades, the labor income of a craftsman i in trade j is:

$$I_{ij} = q_{ij} \left(1 - \alpha \right) \frac{Y}{L} \left(\frac{L_j}{L} \right)^{\frac{1}{\lambda} - 1}.$$

Apprentices choose the most attractive trade. In equilibrium, the net benefit of joining as an apprentice is equalized across trades, so that for all j we have:

$$\mathbb{E}\, I'_{ij} - p_j m_j = \mathbb{E}\, q'_{ij} \left(1 - \alpha \right) \frac{Y'}{L'} - p\, m. \tag{21}$$

35

Collusion among masters in a given guild leads to social costs and benefits compared to the clan equilibrium. The costs are the usual downsides from limited competition; the guild has an incentive to raise prices and limit entry. Guilds enforced labor market monopsonies, and as a result often limited the number of apprentices that each master was allowed to take on at one time, specified the number of years each apprentice had to spend with his master, or even stipulated time periods that had to elapse between taking on one apprentice and the next (Trivellato 2008, p. 212; Kaplan 1981, p. 283). The purpose of these constraints was to limit supply and increase exclusionary rents, which for our analysis means that technological progress is slowed down compared to a market equilibrium.[27] However, guilds operated across different dynasties and thus represented the full range of knowledge in the given trade. If the guild also enforced apprenticeship contracts (in the same fashion as in the clan equilibrium above), there was more scope for knowledge accumulation. Thus, in the absence of strong centralized contract enforcement institutions (i.e., if the clan and not the market was the relevant alternative), the guild had a genuinely positive role to play.[28]

Consider the choice of a guild j of setting the price of apprenticeship p_j within the trade, or equivalently, of choosing the number a_j of apprentices per master. The guild maximizes the utility of the masters in the trade. If the guild lowers a_j, the effective supply of craftsmen's labor in trade j in the next generation goes down. Due to limited substitutability across trades, this increases future craftsmen's income in the trade, and thus the price p_j that today's apprentices are willing to pay. Thus, as in a standard monopolistic problem, the guild will raise p_j to a level above the marginal cost of training apprentices. The maximization problem of the guild can be expressed as:[29]

$$\max_{a_j} \left\{ p_j \, a_j - \delta(a_j) + \kappa \, a_j \right\} \tag{22}$$

---

[27]We focus on the role of guilds in limiting entry because this is what matters for growth in our setting. Another anti-competitive role of guilds is to limit competition in product markets (Ogilvie 2014, 2016). In our model, this feature does not arise because we abstract from an intensive margin of labor supply.

[28]This feature provides a contrast between our work and other recent research on the economic role of guilds, such as Desmet and Parente (2014).

[29]For simplicity, and realistically for the European case, we assume that the children of masters in trade j will look for apprenticeship in other trades. This can be rationalized by a small role for "talent" in choosing trades.

subject to:

$$S_j N' m_j = N a_j,$$

$$p_j = \gamma \frac{\partial \mathbb{E}\, I'_{ij}}{\partial m_j},$$

$$\mathbb{E}\, I'_{ij} - p_j m_j = (1 - \alpha) \frac{Y'}{N'} - p\, m.$$

Here S_j is the endogenous relative share of apprentices choosing to join trade j. We have $S_j = 1$ in equilibrium; however, the guild solves its maximization problem taking the behavior of all other trades as given, so that S_j varies with p_j and a_j in the maximization problem of the guild. The second constraint represents the optimal behavior of parents sending their children to trade j (equalizing p_j to the marginal benefit of training with an additional master). The third constraint stems from the mobility of apprentices across trades (from (21)). These two equations represent the two market forces limiting the power of the guild. Notice that Y'/N' is exogenous for the guild j, because each trade is of infinitesimal size.

Lemma 2. *At the symmetric equilibrium, the solution to the maximization problem (22) satisfies:*

$$\delta'(a) - \kappa = \Omega(m)\, \gamma \theta (1 - \alpha) \frac{1}{m + \nu} \frac{Y'}{N'} \tag{23}$$

with $\Omega(m) < 1$.

Proof. See Appendix G. ∎

Thus, the condition determining equilibrium in the apprenticeship market is of the same form as in the market equilibrium (see Lemma 1), but with the benefit from apprenticeship scaled down by a factor strictly smaller than one. Hence, the extent of apprenticeship (and productivity growth) will be lower compared to the market equilibrium. In the limit where trades become perfect substitutes, $\lambda \to 1$, we have that $\Omega(m) \to 1$, i.e., guilds have no market power and the problem of the guild leads to the same solution as the market (Lemma 1).

We can now characterize the balanced growth path in the guild equilibrium.

Proposition 5 (Balanced Growth Path in Guild Equilibrium).
The unique balanced growth path in the guild equilibrium has the following properties:

(a) *The number of apprentices per master a^G solves (23):*

$$\delta'(a^G) - \kappa = \Omega\left(\frac{a^G}{n^G}\right) \gamma\theta(1-\alpha)\frac{1}{(a^G/n^G+\nu)}y^G, \tag{24}$$

and the number of masters per child m^G is the solution to $m^G = a^G/n^G$.

(b) *The growth factor g^G of knowledge k is given by:*

$$g^G = m^G + \nu.$$

(c) *The growth factor n^G of population N is given by:*

$$n^G = \left(g^G\right)^{\frac{(1-\alpha)\theta}{\alpha}}.$$

(d) *Income per capita is constant and satisfies:*

$$y^G = \frac{\left(g^G\right)^{\frac{(1-\alpha)\theta}{\alpha}}}{\bar{n}\,s}.$$

The guild equilibrium yields lower growth in productivity and population and lower income per capita than does the market equilibrium.

Proof. See Appendix H. ∎

The guild equilibrium is represented in Figure 4, where the apprenticeship market is described by Equation (24). This relationship is similar to the apprenticeship market condition in the market equilibrium, but with a shift to the left because of the market power of the guild, represented by the term $\Omega(\cdot)$.

For explaining the rise of European technological supremacy, the key comparison is between the growth performance of the guild equilibrium (which we view as representing Europe for much of the period from the Middle Ages to the Industrial Revolution) and the clan equilibrium (a feature of other regions such as China, India, and the Middle East). There are forces in both directions; guilds foster growth compared to clans because knowledge can disseminate across ancestral lines, but at the same time the anticompetitive behavior of guilds may limit access to apprenticeship. For this reason, the ranking of growth rates depends on parameters. The guild will lead to faster growth if λ is sufficiently small, because a low λ (close to 1) implies that guilds have little market
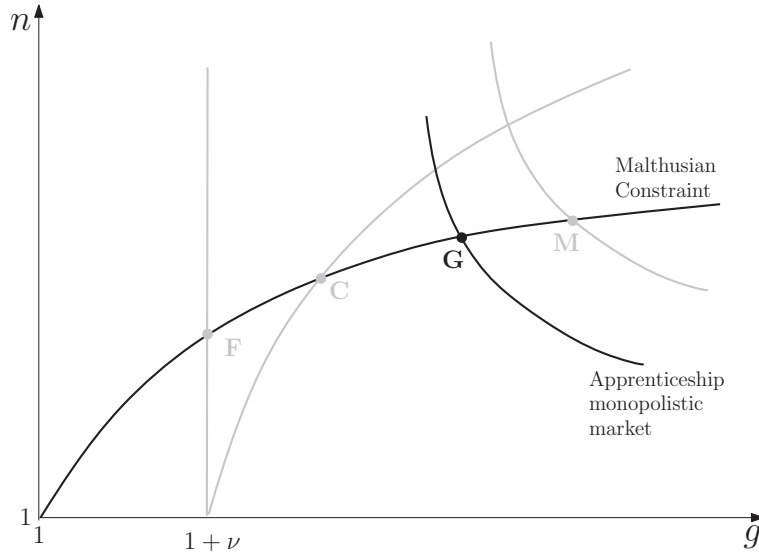
Figure 4: Productivity and Population Growth in the Guild (**G**) Equilibrium

power, so that the guild equilibrium is close to the market equilibrium. Moreover, the guild also generates faster growth if the rate of innovation ν (i.e., the relative efficiency of new versus existing ideas) is close to zero. In this case, most growth is due to the dissemination of existing ideas rather than to the generation of new knowledge, and guilds dominate clans in terms of dissemination (recall that the growth rate in the clan equilibrium is zero if $\nu = 0$).

Perhaps the most important comparison is that the guild would always lead to more growth than the clan if the number of masters m were the same in both systems. In the guild, conditional on m, masters are selected in the best possible way (namely as independent draws from the distribution of knowledge, which maximizes the probability that something new can be learned from an additional master). While the guild may limit access to apprenticeship, it does benefit from allowing for an efficient choice of masters, because this raises the expected benefit of learning from masters and hence the price apprentices are willing to pay. Put differently, the guild distorts only the quantity, but not the quality of apprenticeship. In contrast, in the clan the knowledge of the multiple masters that a given apprentice learns from is necessarily correlated, given that all masters started out with the same initial knowledge available in the clan. Thus, for a given m, in a clan apprentices are exposed to a smaller variety of ideas, and (on average) they learn less. Hence, the only scenario where the clan could generate more growth than the guild is where the market power of guilds is so strong that they would re-

39

duce m to well below the level prevalent in the clan. If anything, the historical evidence points in the opposite direction. Through the multiple interactions that apprenticeship and journeymanship provided, the European guild system is likely to have offered at least as many learning opportunities as the contemporary clan based system did. From the perspective of our model, faster technological progress in Western Europe compared to other world regions would then be the necessary consequence.

4.6 Apprenticeship Institutions and Growth in a Parameterized Economy

We now illustrate our results with a parameterized example of the model economy. We do not formally calibrate the model, but choose parameter values that yield broadly plausible growth rates for the historical period considered. One period (generation) is interpreted as 25 years. We first set $\alpha = 0.8$, $\theta = 0.25$, $\gamma = 0.1$, $\bar{n} = 2$, $s = 7.5$, $o = 3$, $\kappa = 0.02$, and $\lambda = 4$. We then set ν (the relative efficiency of new ideas) so as to reproduce a growth rate of population of 0.86 percent per generation in the family equilibrium, which matches the estimated growth of population between 10000 BCE and 1000 CE in Clark (2007), Table 7.1. This yields $\nu \approx 0.15$. We set the cost of training apprentices such that the number of masters per apprentice m is identical in the clan and guild equilibria, which yields $\bar{\delta} \approx 0.019$. It would be more realistic to allow for a higher m in the guild equilibrium, but equalizing m across the institutional regimes allows us to isolate the additional growth in the guild equilibrium, compared to the clan equilibrium, that arises solely out of the increased variety in masters' knowledge. Any growth effects due to a higher m in the guild would be additional to this effect.

	$g - 1$	$n - 1$	m	y
Family Equilibrium (**F**)	14.7%	0.86%	1	6.724
Clan Equilibrium (**C**)	14.9%	0.87%	1.018	6.725
Guild Equilibrium (**G**)	16.4%	0.96%	1.018	6.730
Market Equilibrium (**M**)	17.7%	1.02%	1.030	6.735

Table 1: Balanced Growth Paths for Different Apprenticeship Institutions in Parameterized Economy ($g - 1$ is productivity growth; $n - 1$ is population growth, and also growth in total output; m is the number of masters each apprentice learns from; y is income per capita)

Table 1 displays the balanced growth rates for knowledge k and population N under each apprenticeship institution, together with the number of masters per apprentice m

and income per adult y. Notice that since y is constant in the balanced growth path, the growth rate of total output Y is equal to the growth rate of population N. We find that productivity growth, population growth, output growth, and income per capita are all increasing as we proceed from family to clan, guild, and ultimately the market. Unlike in Malthusian theories with fixed productivity growth, in our model the long-run level of income per capita is endogenous and depends on learning institutions.

In terms of the growth performance of the different institutional regimes, we notice that the growth advantage of the clan compared to the family is small. In contrast, guild and market yield substantially higher growth rates than either family or clan. The market yields the highest growth rate. However, moving from clan to guild already generates 60 percent of the growth rate differential between clan and market, despite the fact that (by our choice of parameterization) the number of apprentices is identical in the clan and guild equilibria.[30] Hence, the easier dissemination of knowledge for a given m in a system unconstrained by bloodlines accounts for the majority of the overall growth effect of better institutions. Moving from guild to market yields an additional growth effect through a higher m (because in the market system, guilds are not able to restrict access to apprenticeship). The variation in m between the apprenticeship institutions is small in our example (from 1 in the family to 1.03 in the market). If we lowered the cost of training apprentices to generate higher (and arguably more realistic) values for m under the guild and market institutions, the differences in growth rates across regimes would be even larger.[31]

5 The Rise of Europe's Technological Primacy

A central question about pre-industrial economic growth is how, in the centuries leading up to the Industrial Revolution, Western Europe pulled ahead of other world regions. It came to achieve technological primacy over the previous leaders, and on the eve of the

---

[30]Notice that in all cases, the number of masters per apprentice m is either equal to one or close to one. While we treat m in the model as a continuous variable, an alternative interpretation is that even in the more efficient instititional regimes, relatively few workers benefit from learning from multiple masters, generating a low average m in the aggregate.

[31]Greif and Tabellini (2015) discuss the dynamic implications of a somewhat similar issue. In their paper, different equilibria are determined by how people choose their location on the basis of their types (or moral beliefs), which are either "clannish" or "general." Like skills, moral beliefs are transmitted between generations, but rather than being taught on a one-to-one basis, beliefs result from vertical socialization and the environment in a cultural evolution model. Moral beliefs in their paper are measured by a willingness to contribute to public goods, whereas we are interested in the quality of productive skills. In our model we do not rely on heterogeneous preferences and what is driving the different equilibria are the different institutions the economy relies on to enforce the master-apprentice contract.

Industrial Revolution living standards had become substantially higher than elsewhere. A number of researchers have cited the region's faster growth as a key precondition for successful industrialization.[32]

As our analysis above makes clear, in our view apprenticeship institutions that promoted the dissemination of knowledge lay at the heart of Western Europe's success. Many of the guild arrangements supported the spread of technological knowledge beyond the boundaries of individual guilds, a critical factor in the diffusion of technology across the European continent.[33] Beyond the practice of tramping during the *Wanderjahre*, guilds also supplied waystations or *Herbergen* to host itinerant journeymen, who sometimes were lodged at the expense of the guild. Local artisans would interview these artisans, and sometimes hire them (Farr 2000, p. 212). Trained artisans were a mobile element in Europe. Some were highly mobile journeymen who moved across linguistic and national boundaries; others were permanent immigrants, lured by incentives or immigrants to new settlements. Technology diffused through Europe with skilled craftsmen in search of a livelihood. Given the localized nature of control guilds wielded, there seems to be no serious way they could have prevented this diffusion from happening (Reith 2008).

What remains to be determined is why Europe adopted superior institutions such as the guild and ultimately the market, whereas other regions failed to do so. We now consider mechanisms that explain transitions over time between different apprenticeship institutions.

In our view, the adoption of superior institutions in Europe is rooted in differences in initial conditions. As we mentioned earlier, most of the non-European pre-industrial economies were characterized by the clan equilibrium. The importance of clans in China has recently been emphasized in the work of Avner Greif with different coauthors (e.g., Greif and Tabellini 2010, Greif, Iyigun, and Sasson 2012, and Greif and Iyigun 2013). More generally, Kumar and Matsusaka (2009) report an array of historical evidence documenting the preindustrial importance of kinship networks in China, India, and the Islamic world. In contrast to the rest of the world, in Europe the nuclear family came to dominate (corresponding to the family equilibrium in our model). It is clear that by

---

[32]The rise of Europe in the centuries leading up to the Industrial Revolution is also the subject of two recent papers by Voigtländer and Voth (2013a, 2013b). However, they emphasize demographic changes, whereas our analysis is about differences in productivity growth.

[33]Our theoretical analysis implicitly allows for such wide diffusion by assuming that guilds comprise *all* masters in a given trade, rather than being limited to specific cities or regions.

1500, extended families (or what we might call "clans") had become less visible in Europe, and especially in the Western part (Shorter 1975, p. 284). Peter Laslett, who has done more than anyone to establish this view, referred to the typical European family as the conjugal family unit, couple plus offspring (Laslett and Wall 1972). When, and even more so why, this pattern became so dominant in Europe remains to this day a debated question.[34] To some extent it may have been encouraged by policies of the Western Christian church, as Greif and Tabellini argue. In Europe the Christian church actively discouraged practices that sustained kinship groups. The existence of institutions that encouraged the cooperation among non-kin, such as manors and monasteries, may have been equally important. By the early Middle Ages the nuclear family already dominated in some areas.[35]

Why did (nuclear) family-based Europe adopt better institutions over time, while clan-based regions did not? One potential explanation is that it is precisely Europe's starting point in the low-growth family equilibrium that fostered the more rapid adoption of superior institutions. If adopting the guild or market systems is costly, the incentive for adoption depends on the the performance of the existing institutions. In our view, other world regions had less to gain from adopting new institutions, given that the clan-based system performed well for most purposes.

To formalize this possibility, consider the option of adopting the guild system at fixed per-family cost of $\mu(N)$. We let this cost depend on the density of population, with $\mu'(N) < 0$ reflecting the idea that the adoption of guilds is cheaper when density is high (in line with the fact that the incidence of guilds increases with population density, see De Munck, Lourens, and Lucassen 2006). This cost $\mu(N)$ can either be seen either as an aggregate cost of setting up guilds or courts, or linked to an individual decision, i.e., the cost of moving from a small town to a larger city where contract enforcement institutions are in place.

Formally, we need to compare the utility of the parents from keeping the current system, $u^{F \to F}$ and $u^{C \to C}$ with the one of adopting the guild based apprenticeship, $u^{F \to G}$ and $u^{C \to G}$. Let us consider two economies having the same population N_0 and knowledge k_0, one

---

[34]The dominance of the nuclear family went together with the enforcement of strict monogamy, when it became infeasible for men to simultaneously father children from multiple women, and remarriage was only possible after widowhood, see de la Croix and Mariani (2015).

[35]Mitterauer (2010) describes two signs of the emergence of the nuclear family: the distinction between paternal and maternal relatives disappeared from the Romance languages by 600 CE (and from other European languages soon after); and spiritual kinships analogous to blood kinships were established (such as godmother and godfather).

in the family system, the other in the clan system. The distribution of income is thus the same in these two economies, as is mean income y_0 and the number of children n_0. Adults have to decide whether to pay the cost μ to adopt the guild. If the guild is adopted, the equilibrium price of apprenticeship will be p_0, the number of apprentices per master will be a_0, and the number of masters teaching one apprentice will be m_0. The income of the children under the guild system will be given by: $y^{\text{F}\to\text{G}} = y^{\text{C}\to\text{G}} \equiv y_1^{\text{G}}$. Let us now write the utility in the four cases:

$$
\begin{aligned}
u^{\text{F}\to\text{F}} &= y_0 + \gamma\, n_0\, y_1^{\text{F}} + \kappa\, n_0 - \delta(n_0) \\
u^{\text{F}\to\text{G}} &= y_0 + \gamma\, n_0\, y_1^{\text{G}} + \kappa\, a_0 - \delta(a_0) - \mu(N_0) \\
u^{\text{C}\to\text{C}} &= y_0 + \gamma\, n_0\, y_1^{\text{C}} + \kappa\, (n_0)^{o+1} - \delta((n_0)^{o+1}) \\
u^{\text{C}\to\text{G}} &= y_0 + \gamma\, n_0\, y_1^{\text{G}} + \kappa\, a_0 - \delta(a_0) - \mu(N_0)
\end{aligned}
$$

The following propositions gives the main result.

Proposition 6 (**Transition from Family and Clan to Guild**).
Consider two economies with the same initial knowledge and population, one in the family equilibrium, and one in the clan equilibrium. If $\lim_{N\to 0}\mu(N) = \infty$ and $\lim_{N\to\infty}\mu(N) = 0$, there exist population thresholds $\underline{N}$ and $\overline{N}$, with $\underline{N} < \overline{N}$, such that:

> ▷ *if $N_0 < \underline{N}$, none of the economies adopt the guild institution.*
> ▷ *if $\underline{N} \le N_0 \le \overline{N}$, only the economy in the family equilibrium adopts the guild institution.*
> ▷ *if $\overline{N} < N_0$, both economies adopt the guild institution.*

Proof. See Appendix I. ∎

Given equal populations, the incentive to pay the fixed cost will be lower when the initial economic system is more successful, i.e., a clan-based economy will be less likely to adopt than a family-based economy.[36]

Take now two hypothetical economies starting with the same low level of population. Suppose that one of them starts in the family equilibrium, whereas in the other the clan equilibrium prevails. In both economies, population is low and the guild equilibrium is not adopted, but there is still some technical progress and population grows. Given

---

[36]This explanation applies earlier work by Avner Greif (see in particular Greif 1993 and Greif 1994) on institutional change to the issue of human capital and knowledge transmission.

Proposition 3, population growth is higher in the clan economy. The question is which economy will first reach the population threshold that makes adopting the market optimal. The family economy has a lower threshold value, but, as it grows more slowly, it is not clear that it will adopt the guild first. A possible trajectory is the one shown in Figure 5. Here, the family economy adopts the guild earlier, at date t_1, which allows it to catch up and overtake the c economy. Later on, the clan economy may or may not reach its own threshold above which it is optimal to adopt the guild, depending on the properties of the cost function $\mu(\cdot)$, and in particular how it behaves when population becomes large. If $\lim_{N \to \infty} \mu(N) = 0$, the guild will be adopted for sure (which is the case covered in Proposition 6). But if $\lim_{N \to \infty} \mu(N) > 0$ (which is the case, for instance, if the total cost of setting up guilds includes a fixed cost per family), the economy may stay permanently in the clan equilibrium. The case displayed in the picture is where the economy that starts out in the clan equilibrium reaches the threshold at some later date t_2.

Proposition 7 (Clan as an Absorbing State).
If

$$\lim_{N \to \infty} \mu(N) > \gamma n^{c}(y_1^{G} - y^{c}) + \kappa(a_1^{G} - (n^{c})^{o+1}) - \delta(a_1^{G}) + \delta((n^{c})^{o+1}),$$

the economy in the clan equilibrium never adopts the guild.

Here the values of n^{c} and y^{c} are defined in Proposition 3, and y_1^{G}, a_1^{G} are values from the guild equilibrium after one period, starting from the clan balanced growth path as the initial condition. The proposition holds because, in a Malthusian context, income per person y^{c} and y_1^{G} remains bounded.

In reality, complementary mechanisms are likely to have also contributed to the failure of clan-based economies to adopt more efficient apprenticeship institutions. The clan-based organization had many advantages over the family other than faster knowledge growth; indeed, most economic and social life was organized around the clan. One specific aspect was that the clan adhered to what Greif and Tabellini call "limited morality"—a loyalty to kin but not to others. Such institutions have obvious attractions, such as an advantage in intra-group cooperation, the supply of public goods, and mutual insurance. But they have a comparative disadvantage in sustaining broader intergroup cooperation. In terms of economic efficiency, the two arrangements of family and clan therefore have clear tradeoffs. The clan economizes on enforcement costs, but at the cost of economies of scale and pluralism. The bottom line is that for a successful
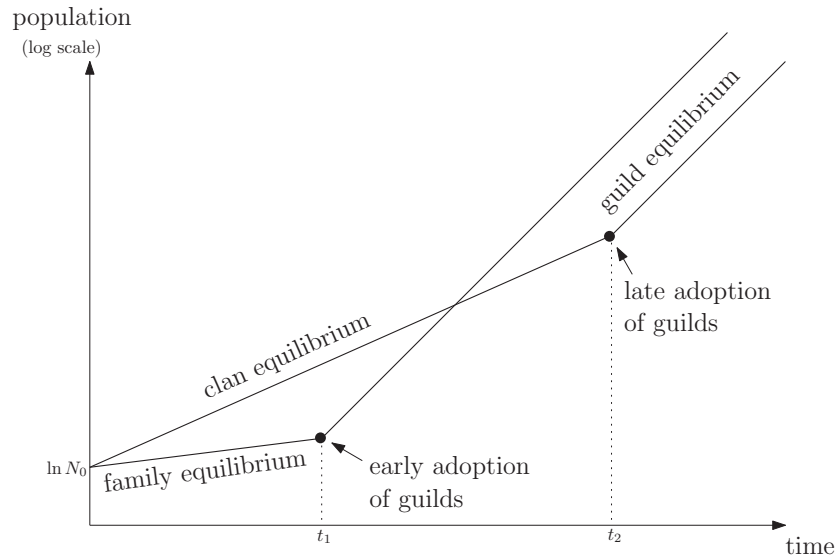
Figure 5: Possible Dynamics of Two Economies Starting from the Same N_0

clan-based economy, the cost of giving up the existing system of social organization (in favor of the guild system) is likely to have been much higher than what our stylized model suggests.

Another dimension is that the dominance of the nuclear family in Europe created a need early on for organizations that cut across family lines. Guilds were independent of families, but they had many antecedents that had a similar legal status (such as monasteries, universities or independent cities). Hence, earlier institutional developments may have made the adoption of guilds in Europe much cheaper compared to clan-based societies.

Still other factors also may have been at work in specific regions. A striking difference between China and Europe before the Industrial Revolution is in settlement patterns. China was, as Greif and Tabellini point out, a land of clans, but much less than Europe a land of cities. As Rosenthal and Wong (2011, p. 113) stress, Chinese manufacturing was much less concentrated in cities than it was in Europe—a difference they attribute to the dissimilar warfare patterns. In China the main threat came not from one's neighbors but from invading nomads from the steppe; hence the need for a Great Wall. Cities were walled to some extent, but walled cities were far fewer than in Europe, and the walls served more as symbols than as protection from attack. As much as 97 percent of the Chinese population lived outside the walled cities. This difference in urbanization is an important clue to why European institutions evolved in a different way. If the cost of adopting guilds depends on population density, the "effective" population density

46

would have been much higher in Europe, because craftsmen were concentrated in small urban areas. In the model above, that difference would be represented as a lower level of the cost function $\mu(N)$ for a given overall population.

In our analysis of institutional transitions, we focus on the introduction of apprenticeships and guilds in Western Europe. An important topic for future research is to consider also the ensuing transition from guild to market, which results in even more rapid growth. If we are comparing Europe with the world of clans, we must note that all-powerful guilds were not ubiquitous in Europe, and that by the middle of the seventeenth century craft guilds were declining in many areas. In the Netherlands, in England, and even to some extent in France, the power of guilds to impose restrictions on entry and to control product markets faded in the eighteenth century. It was then that "free trade" regions (i.e., exempted from guild control) emerged, such as the famous one in the Faubourg St. Antoine near Paris (Horn 2015, pp. 1–3). In other words, not only did Europe adopt guilds, a superior set of institutions for transmitting skills relative to clans, but also, Europe was in transit to a market system which was even better at it.

6   Conclusion

In this paper, we have examined sources of productivity growth in pre-industrial societies, in order to explain the economic ascendency of Western Europe in the centuries leading up to industrialization. We developed a model of person-to-person exchanges of ideas, and argued that apprenticeship institutions that regulate the transmission of tacit knowledge between generations are key for understanding the performance of pre-industrial economies.

In our analysis, we have put the spotlight on differences across institutions in the dissemination of knowledge. Of course, a second channel of productivity growth is innovation, i.e., the creation of entirely new knowledge. Our analysis does allow for innovation in the form of new ideas, but we have held this aspect of productivity growth constant across institutions. A natural extension of our work would be to examine how the institutional differences we identify here as driving differences in the dissemination of knowledge may affect incentives for original innovation. The importance of highly skilled craftsmen for the innovative activities that led to the Industrial Revolution has become an important theme in the industrialization literature. Indeed, some scholars such as Hilaire-Pérez (2007) and Epstein (2013) have argued that rising artisanal skill levels and the high level of innovation among the most sophisticated craftsmen alone could

have fostered the Industrial Revolution. While such an extreme view slights the contribution of codifiable knowledge and formal science, there is no question that high-ability artisans were a pivotal element in the rise of modern technology, and that Britain's leadership rested to a great extent on the advantage it had in skilled workers (Kelly, Mokyr, and Ó Gráda 2014). It is more realistic to argue that there were strong complementarities between the growth of modern science in the seventeenth and eighteenth centuries and the existence of highly refined skills. Advances were made by a literate and educated elite, the classic example of upper-tail human capital (de la Croix and Licandro 2015, and Squicciarini and Voigtländer 2015). Increasing longevity, moreover, in the mid-seventeenth century may have stimulated further investment in the human capital of this elite and facilitated the diffusion of their knowledge. Yet, just as importantly, these highly educated people interacted with the most skilled and dexterous craftsmen (Meisenzahl and Mokyr 2012).

A powerful example of this complementarity is the British watch industry in the eighteenth century. Watchmaking was a high-level skill, originally regulated by a guild (the Worshipful Company of Clockmakers, one of the original livery companies of the City of London) but by 1700 more or less free of guild restrictions. Training occurred exclusively through master-apprentice relations. In the seventeenth century, the industry experienced a major technological shock by the invention of the spiral-spring balance in watches by two of the best minds of the seventeenth century, Christiaan Huygens and Robert Hooke (ca. 1675). No similar macro-invention occurred over the subsequent century, yet the real price of watches fell by an average of 1.3 percent a year between 1685 and 1810 (Kelly and Ó Gráda 2016). As Kelly and Ó Gráda note, "Once this conceptual breakthrough occurred, England's extensive tradition of metal working and the relative absence of restrictions on hiring apprentices, along with an extensive market of affluent consumers, allowed its watch industry to expand rapidly"(p. 5). An eighteenth century observer noted that for watchmaking an apprentice needed at least 14 years (or fewer if he was "tolerably acute") and that to be truly skilled he needed to learn a "smattering of mechanics and mathematics"—presumably skills that were taught by the master (Campbell 1747, p. 252). We leave for future research an exploration of the various complementarities between the dissemination of the creation of knowledge within a model of person-to-person exchanges of ideas.

References

Aghion, Philippe, and Peter Howitt. 1992. "A Model of Growth through Creative Destruction." *Econometrica* 60 (2): 323–51.

Alvarez, Fernando E., Francisco J. Buera, and Robert E. Lucas, Jr. 2008. "Models of Idea Flows." NBER Working Paper 14135.

———. 2013. "Idea Flows, Economic Growth, and Trade." NBER Working Paper 19667.

Ashraf, Quamrul, and Oded Galor. 2011. "Dynamics and Stagnation in the Malthusian Epoch." *American Economic Review* 101 (5): 2003–41.

Barro, Robert J., and Gary S. Becker. 1989. "Fertility Choice in a Model of Economic Growth." *Econometrica* 57 (2): 481–501.

Belfanti, Carlo Marco. 2004. "Guilds, Patents, and the Circulation of Technical Knowledge." *Technology and Culture* 45 (3): 569–89.

Ben Zeev, Nadav, Joel Mokyr, and Karine Van Der Beek. 2015. "Flexible Supply of Apprenticeship in the British Industrial Revolution." Unpublished Manuscript, Northwestern University.

Brooks, Christopher. 1994. "Apprenticeship, Social Mobility and the Middling Sort, 1550–1800." In *The Middling Sort of People: Culture, Society and Politics in England, 1550-1800*, edited by Jonathan Barry and Christopher Brooks, 52–83. London: Palgrave Macmillan.

Campbell, R. 1747. *The London Tradesman*. London: Printed by T. Gardner.

Clark, Gregory. 2007. *A farewell to alms: a brief economic history of the world*. Princeton: Princeton University Press.

Cowan, Robin, and Dominique Foray. 1997. "The Economics of Codification and the Diffusion of Knowledge." *Industrial and Corporate Change* 6 (3): 595–622.

Davids, Karel. 2003. "Guilds, Guildmen and Technological Innovation in Early Modern Europe: The Case of the Dutch Republic." Economy and Society in the Low Countries Working Papers, No. 2.

———. 2007. "Apprenticeship and Guild Control in the Netherlands, c. 1450-1800." In *Learning on the Shop Floor: Historical Perspectives on Apprenticeship*, edited by Steven L. Kaplan Bert De Munck and Hugo Soly, 65–84. New York: Berghahn Books.

——. 2013. "Moving Machine-makers: Circulation of Knowledge on Machine-building in China and Europe between c. 1400 and the Early Nineteenth century." Chapter 6 of *Technology, Skills and the Pre-Modern Economy in the East and the West*, edited by Jan L. van Zanden and Marten Prak. Boston: Brill.

Davies, Margaret Gay. 1956. *The Enforcement of English Apprenticeship: a Study in Applied Mercantilism, 1563-1642*. Cambridge, MA: Harvard University Press.

de la Croix, David, and Matthias Doepke. 2003. "Inequality and Growth: Why Differential Fertility Matters." *American Economic Review* 93 (4): 1091–113.

de la Croix, David, and Omar Licandro. 2015. "The Longevity of Famous People from Hammurabi to Einstein." *Journal of Economic Growth* 20:263–303.

de la Croix, David, and Fabio Mariani. 2015. "From Polygyny to Serial Monogamy: A Unified Theory of Marriage Institutions." *Review of Economic Studies* 82 (2): 565–607.

De Munck, B.Bert, Piet Lourens, and Jan Lucassen. 2006. "The Establishement and Distribution of Crafts Guilds in the Low Countries 1000-1800." Chapter 2 of *Crafts Guilds in the Early Modern Low Countries: Work, Power and Representation*, edited by Maarten Prak, Catharina Lis, Jan Lucassen, and Hugo Soly. Aldershot: Ashgate.

De Munck, Bert, and Hugo Soly. 2007. "Learning on the Shop Floor in Historical Perspective." In *Learning on the Shop Floor: Historical Perspectives on Apprenticeship*, edited by Steven L. Kaplan Bert De Munck and Hugo Soly, 3–32. New York: Berghahn Books.

Desmet, Klaus, and Stephen L. Parente. 2014. "Resistance to Technology Adoption: The Rise and Decline of Guilds." *Review of Economic Dynamics* 17 (3): 437–58.

Dittmar, Jeremiah E. 2011. "Information Technology and Economic Change: The Impact of The Printing Press." *The Quarterly Journal of Economics* 126 (3): 1133–1172.

Doepke, Matthias. 2004. "Accounting for Fertility Decline During the Transition to Growth." *Journal of Economic Growth* 9 (3): 347–83.

Dunlop, O. Jocelyn. 1911. "Some Aspects of Early English apprenticeship." *Transactions of the Royal Historical Society, Third Series* 5:193–208.

——. 1912. *English Apprenticeship and Child Labor*. New York: MacMillan.

Eaton, Jonathan, and Samuel Kortum. 1999. "International Technology Diffusion: Theory and Measurement." *International Economic Review* 40 (3): 537–70.

Epstein, Stephan R. 2008. "Craft Guilds, the Theory of the Firm, and the European Economy, 1400-1800." In *Guilds, Innovation and the European Economy, 1400-1800*, edited by Stephan R. Epstein and Maarten Prak, 52–80. Cambridge: Cambridge University Press.

Epstein, Stephan R. 2013. "Transferring Technical Knowledge and Innovating in Europe, c. 1200-c. 1800." Chapter 1 of *Technology, Skills and the Pre-Modern Economy in the East and the West*, edited by Jan L. van Zanden and Marten Prak. Boston: Brill.

Epstein, Stephan R., and Maarten Prak. 2008. "Introduction: Guilds, Innovation and the European Economy, 1400-1800." In *Guilds, Innovation and the European Economy, 1400-1800*, edited by Stephan R. Epstein and Maarten Prak, 1–24. Cambridge: Cambridge University Press.

Farr, James. 2000. *Artisans in Europe, 1300–1914*. Cambridge: Cambridge University Press.

Fogli, Alessandra, and Laura Veldkamp. 2012. "Germs, Social Networks and Growth." NBER Working Paper 18470.

Foray, Dominique. 2004. *The Economics of Knowledge*. Cambridge, MA: MIT Press.

Galor, Oded. 2011. *Unified Growth Theory*. Princeton: Princeton University Press.

Galor, Oded, and David N. Weil. 2000. "Population, Technology, and Growth: From Malthusian Stagnation to the Demographic Transition and Beyond." *American Economic Review* 90 (4): 806–28.

Greif, Avner. 1993. "Contract Enforceability and Economic Institutions in Early Trade: The Maghribi Traders' Coalition." *American Economic Review* 83 (3): 525–48.

———. 1994. "Cultural Beliefs and the Organization of Society: A Historical and Theoretical Reflection on Collectivist and Individualist Societies." *Journal of Political Economy* 102 (5): 912–50.

———. 2006. "Family Structure, Institutions, and Growth: The Origins and Implications of Western Corporations." *The American Economic Review* 96 (2): 308–312.

Greif, Avner, and Murat Iyigun. 2013. "Social Organizations, Violence, and Modern Growth." *American Economic Review* 103 (3): 534–38.

Greif, Avner, Murat Iyigun, and Diego Sasson. 2012. "Social Institutions and Economic Growth: Why England and Not China Became the First Modern Economy." Unpublished Working Paper, University of Colorado.

Greif, Avner, and Guido Tabellini. 2010. "Cultural and Institutional Bifurcation: China and Europe Compared." *American Economic Review* 100 (2): 135–40.

———. 2015. "The Clan and the Corporation: Sustaining Cooperation in China and Europe." Unpublished Manuscript, Bocconi University.

Hilaire-Pérez, Liliane. 2007. "Technology as Public Culture." *History of Science* 45 Pt. 2 (148): 135–153.

Horn, Jeff. 2015. *Economic Development in Early Modern France*. Cambridge: Cambridge University Press.

Humphries, Jane. 2003. "English Apprenticeship: A Neglected Factor in the First Industrial Revolution." Chapter 3 of *The Economic Future in Historical Perspective*, edited by Paul A. David and Mark Thomas. Oxford: Oxford University Press.

———. 2010. *Childhood and Child Labour in the British Industrial Revolution*. Cambridge Studies in Economic History - Second Series. Cambridge: Cambridge University Press.

Jones, Charles I. 2001. "Was an Industrial Revolution Inevitable? Economic Growth Over the Very Long Run." *The B.E. Journal of Macroeconomics* 1 (2): 1–45 (August).

Jovanovic, Boyan. 2014. "Misallocation and Growth." *American Economic Review* 104 (4): 1149–1171.

Jovanovic, Boyan, and Rafael Rob. 1989. "The Growth and Diffusion of Knowledge." *The Review of Economic Studies* 56 (4): 569–82.

Kaplan, Steven L. 1981. "The Luxury Guilds in Paris in the Eighteenth Century." *Francia* 9:257–98.

Kelly, Morgan, Joel Mokyr, and Cormac Ó Gráda. 2014. "Precocious Albion: A New Interpretation of the British Industrial Revolution." *Annual Review of Economics* 6:363–389.

Kelly, Morgan, and Cormac Ó Gráda. 2012. "The Preventive Check in Medieval and Preindustrial England." *The Journal of Economic History* 72 (04): 1015–1035 (December).

———. 2014. "Living Standards and Mortality Since the Middle Ages." *Economic History Review* 67 (2): 358–381 (05).

———. 2016. "Adam Smith, Watch Prices, and the Industrial Revolution." Forthcoming, Quarterly Journal of Economics.

König, Michael, Jan Lorenz, and Fabrizio Zilibotti. 2015. "Innovation vs. Imitation and the Evolution of Productivity Distributions." Forthcoming, Theoretical Economics.

Kortum, Samuel S. 1997. "Research, Patenting, and Technological Change." *Econometrica* 65 (6): 1389–419.

Kremer, Michael. 1993. "Population Growth and Technological Change: One Million B.C. to 1900." *Quarterly Journal of Economics* 108 (3): 681–716.

Kumar, Krishna B., and John G. Matsusaka. 2009. "From families to formal contracts: An approach to development." *Journal of Development Economics* 90 (1): 106–119.

Lane, Joan. 1996. *Apprenticeship in England 1600-1914*. Boulder: Westview Press.

Laslett, Peter, and Richard Wall, eds. 1972. *Household and Family in Past Time*. Cambridge: Cambridge University Press.

Leunig, Tim, Chris Minns, and Patrick Wallis. 2011. "Networks in the Premodern Economy: The Market for London Apprenticeships, 1600-1749." *The Journal of Economic History* 71 (6): 413–443.

Lis, Catharina, Hugo Soly, and Lee Mitzman. 1994. "'An Irresistible Phalanx:' Journeymen Associations in Western Europe, 1300-1800." *International Review of Social History* 39 (8): 11–52.

Long, Pamela O. 2011. *Artisan/Practitioners and the Rise of the New Sciences, 1400-160*. Cornvallis: Oregon State University Press.

Lucas, Jr., Robert E. 2009. "Ideas and Growth." *Economica* 76 (301): 1–19.

Lucas, Jr., Robert E., and Benjamin Moll. 2014. "Knowledge Growth and the Allocation of Time." *Journal of Political Economy* 122 (1): 1–51.

Lucassen, Jan, Tine de Moor, and Jan Luiten van Zanden. 2008. "The Return of the Guilds: Towards a Global History of the Guilds in Pre-Industrial Times." In *The Return of the Guilds*, edited by Jan Lucassen, Tine de Moor, and Jan Luiten van Zanden, 5–18. Cambridge: Cambridge University Press.

Luttmer, Erzo G. J. 2007. "Selection, Growth, and the Size Distribution of Firms." *The Quarterly Journal of Economics* 122 (3): 1103–1144.

———. 2015. "An Assignment Model of Knowledge Diffusion and Income Inequality." Unpublished Manuscript, University of Minnesota.

Meisenzahl, Ralf R., and Joel Mokyr. 2012. "The Rate and Direction of Invention in the British Industrial Revolution: Incentives and Institutions." In *The Rate and Direction of Innovation*, edited by In Scott Stern and Joshua Lerner, 443–479. Chicago: University of Chicago Press.

Minns, Chris, and Patrick Wallis. 2013. "The Price of Human Capital in a Pre-industrial Economy: Premiums and Apprenticeship Contracts in 18th century England." *Explorations in Economic History* 50 (3): 335–350.

Mitterauer, Michael. 2010. *Why Europe?: The Medieval Origins of Its Special Path*. Chicago: University Of Chicago Press.

Mokyr, Joel. 2002. *The Gift of Athena. Historical Origins of the Knowledge Economy*. Princeton: Princeton University Press.

———. 2008. "The Institutional Origins of the Industrial Revolution." In *Institutions and Economic Performance*, edited by Elhanan Helpman, 64–119. Cambridge MA: Harvard University Press.

Moll-Murata, Christine. 2013. "Guilds and Apprenticeship in China and Europe: The Jingdezhen and European Ceramics Industries." Chapter 7 of *Technology, Skills and the Pre-Modern Economy in the East and the West*, edited by Jan Luiten van Zanden and Marten Prak. Boston: Brill.

Nagata, Mary Louise. 2007. "Apprentices, Servants and Other Workers: Apprenticeship in Japan." In *Learning on the Shop Floor: Historical Perspectives on Apprenticeship*, edited by Steven L. Kaplan Bert De Munck and Hugo Soly, 35–45. New York: Berghahn Books.

———. 2008. "Brotherhoods and Stock Societies: Guilds in Pre-modern Japan." In *The Return of the Guilds*, edited by Jan Lucassen, Tine de Moor, and Jan Luiten van Zanden, 121–142. Cambridge: Cambridge University Press.

Ogilvie, Sheilagh. 2004. "Guilds, Efficiency and Social Capital: Evidence from German Proto-industry." *Economic History Review* 57 (2): 286–333.

———. 2014. "The Economics of Guilds." *Journal of Economic Perspectives* 28 (4): 169–92 (Fall).

———. 2016. "The European Guilds: an Economic Assessment." Unpublished Book Manuscript.

Perla, Jesse, and Christopher Tonetti. 2014. "Equilibrium Imitation and Growth." *Journal of Political Economy* 122 (1): 52–76.

Prak, Maarten. 2013. "Mega-structures of the Middle Ages: The Construction of Religious Buildings in Europe and Asia, c.1000-1500." Chapter 4 of *Technology, Skills and the Pre-Modern Economy in the East and the West*, edited by Jan Luiten van Zanden and Marten Prak. Boston: Brill.

Reith, Reinhold. 2007. "Apprentices in the German and Austrian Crafts in Early Modern Times: Apprentices as Wage Earners?" In *Learning on the Shop Floor: Historical Perspectives on Apprenticeship*, edited by Steven L. Kaplan Bert De Munck and Hugo Soly, 179–99. New York: Berghahn Books.

———. 2008. "Circulation of Skilled Labour in Late Medieval and Early Modern Central Europe." In *Guilds, Innovation and the European Economy, 1400–1800*, edited by S. R. Epstein and Maarten Prak, 114–142. Cambridge University Press.

Robert, Leeson. 1979. *Travelling Brothers*. London: George Allen & Unwin.

Roberts, Lissa, and Simon Schaffer. 2007. "Preface." In *The Mindful Hand: Inquiry and Invention from the late Renaissance to early Industrialization*, edited by Simon Schaffer Lissa Roberts and Peter Dear, xiii–xxvii. Amsterdam: Royal Netherlands Academy of Arts and Sciences.

Romer, Paul M. 1990. "Endogenous Technological Change." *Journal of Political Economy* 98 (5): S71–S102.

Rosenthal, Jean-Laurent, and R. Bin Wong. 2011. *Before and Beyond Divergence: The Politics of Economic Change in China and Europe*. Cambridge, MA: Harvard University Press.

Roy, Tirthankar. 2013. "Apprenticeship and Industrialization in India, 1600-1930." Chapter 2 of *Technology, Skills and the Pre-Modern Economy in the East and the West*, edited by Jan Luiten van Zanden and Marten Prak. Boston: Brill.

Rushton, Peter. 1991. "The Matter in Variance: Adolescents and Domestic Conflict in the Pre-Industrial Economy of Northeast England, 1600-1800." *Journal of Social History* 25 (1): 89–107.

Shorter, Edward. 1975. *The Making of the Modern Family*. New York: Harper Torch Books.

Smith, Steven R. 1973. "The London Apprentices as Seventeenth-Century Adolescents." *Past & Present* 61:149–161.

Spagnolo, Giancarlo. 1999. "Social Relations and Cooperation in Organizations." *Journal of Economic Behavior and Organization* 38 (1): 1–25.

Squicciarini, Mara P., and Nico Voigtländer. 2015. "Human Capital and Industrialization: Evidence from the Age of Enlightenment." *The Quarterly Journal of Economics* 130 (4): 1825–1883.

Stabel, Peter. 2007. "Social Mobility and Apprenticeship in Late Medieval Flanders." In *Learning on the Shop Floor: Historical Perspectives on Apprenticeship*, edited by Steven L. Kaplan Bert De Munck and Hugo Soly, 158–78. New York: Berghahn Books.

Steffens, Sven. 2001. "Le métier volé: transmission des savoir-faire et socialization dans les métiers qualifiés ay XIXe siècle." *Revue du Nord* 15:121–135.

Steidl, Annemarie. 2007. "Silk Weaver and Purse Maker Apprentices in Eighteenth and Nineteenth Century Vienna." In *Learning on the Shop Floor: Historical Perspectives on Apprenticeship*, edited by Bert De Munck, Steven L. Kaplan, and Hugo Soly, 133–57. New York: Berghahn Books.

Trivellato, Francesca. 2008. "Guilds, Technology, and Economic Change in early modern Venice." In *Guilds, Innovation and the European Economy, 1400-1800*, edited by Stephan R. Epstein and Maarten Prak, 199–231. Cambridge: Cambridge University Press.

van Zanden, Jan Luiten. 2009. *The Long Road to the Industrial Revolution: The European Economy in a Global Perspective, 1000-1800*. Boston: Brill.

van Zanden, Jan Luiten, and Marten Prak. 2013a. "Technology and Human Capital Formation in the East and West Before the Industrial Revolution." Chapter 1 of *Technology, Skills and the Pre-Modern Economy in the East and the West*, edited by Jan Luiten van Zanden and Marten Prak. Boston: Brill.

———. 2013b. *Technology, Skills and the Pre-Modern Economy in the East and the West*. Boston MA: Brill.

Voigtländer, Nico, and Hans-Joachim Voth. 2013a. "How the West "Invented" Fertility Restriction." *American Economic Review* 103 (6): 2227–64.

———. 2013b. "The Three Horsemen of Riches: Plague, War, and Urbanization in Early Modern Europe." *The Review of Economic Studies* 80 (2): 774–811.

Vollrath, Dietrich. 2011. "The Agricultural Basis of Comparative Development." *Journal of Economic Growth* 16 (4): 343–370.

Wallis, Patrick. 2008. "Apprenticeship and Training in Premodern England." *The Journal of Economic History* 68 (3): 832–861.

Yildirim, Onur. 2008. "Ottoman Guilds in the Early Modern Era." In *The Return of the Guilds*, edited by Jan Lucassen, Tine de Moor, and Jan Luiten van Zanden, 73–93. Cambridge: Cambridge University Press.

Online Appendices

A Extension with Farmers

In this section, we sketch how the model can be extended by including farm labor as a separate input in production. This extension addresses the concern that in the pre-industrial era, most people were engaged in food production, whereas craftspeople made up a smaller fraction of the population.

The single consumption good (which we interpret as a composite of food and manufactured goods) is produced with a Cobb-Douglas production function with constant return to scale that uses land X, farm labor N_f, and effective craftsmen's labor L as inputs:

$$Y = \left(N_f\right)^{1-\alpha-\beta} L^\beta X^\alpha,$$

with α, $\beta \in (0,1)$. The total amount of land is normalized to one, $X = 1$, and land is owned by farmers.

The aggregate state variables are now three: N_f (population of farmers), N_m (population of craftsmen), and k. Let $N = N_m + N_f$ be the total number of adults. Farmers and craftsmen have the same survival rate and there is no intergenerational mobility across occupations. Hence, the laws of motion for population are:

$$N'_m = n\, N_m, \quad N'_f = n\, N_f, \quad N' = N'_m + N'_f = n\, N.$$

As a consequence, the share of both groups in the total population is constant. We define ρ as

$$\rho = \frac{N_m}{N}.$$

The assumptions of equal population growth and no occupational mobility are made for simplicity. In reality, it is well known that in pre-industrial times cities (where craftsmen were concentrated) experienced much higher mortality than the countryside, so that there was net migration into cities. Allowing for such rural-urban migration could be accommodated in our framework and would leave the main results intact, but would come at the cost of complicating the analysis. Given that our focus is on knowledge transmission rather than urbanization, we abstract from such features here.

Given those two changes to the specification, the rest of analysis carries on. Two new parameters are involved. The market equilibrium condition (18) becomes:

$$\delta'(a^{\text{M}}) - \kappa = \frac{\gamma\theta\beta}{\rho} \frac{1}{a^{\text{M}}/n^{\text{M}} + v} y^{\text{M}}.$$

It becomes easier to analyze the role of parameter α, as now, this one only plays a role in the Malthusian constraint. A low α corresponds to labor-intensive agriculture. In

this case returns to population size decrease at a lower rate, and hence an increase in productivity growth leads to a larger shift in population growth and income per capita compared to the case of a large land share.[37] It modifies the incentives to move to another mode of organizing apprenticeship, as detailed in Proposition 8.
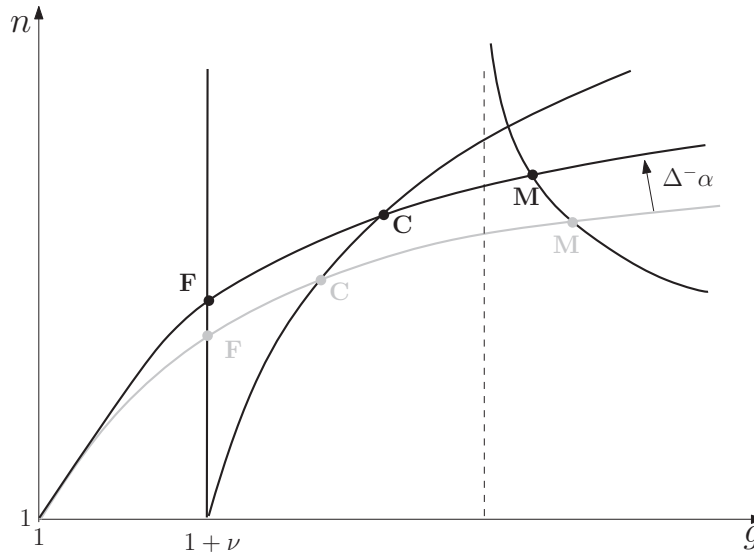

Figure 6: Effect of labor intensive agriculture

Proposition 8 (Effect of Labor-Intensive Agriculture).
If Agriculture is labor intensive (low α), the long-term gains in growth from moving from family to market, $g^M - g^F$, and from clan to market, $g^M - g^C$, are reduced. But the gain from moving from family to clan, $g^C - g^F$, is increased.

Figure 6 shows the result graphically. An implication of this proposition is that a country with labor intensive agriculture has more incentives to adopt the clan than the family.

B Extension with the "Leonardo da Vinci" Assumption

In this section, we allow for the possibility that advanced techniques may be "ahead of their time," in the sense that their full productive value can only be realized at a higher state of aggregate knowledge. For example, Leonardo da Vinci invented a number of machines and devices that could be successfully built only centuries later. To capture this feature in a simple way, we assume that each craftsman has a potential output which is linked to own knowledge h_i, but that the craftsman may be constrained by the average

---

[37]Vollrath (2011) argues that agriculture in pre-industrial China was more labor intensive compared to Europe (due to the possibility of multiple crops per year, wet-field rice production etc.), and that this accounts for part of observed differences in living standards.

state of knowledge in the economy. Specifically, the potential output $\bar{q}_i$ of a craftsman with knowledge h_i is given by:

$$\bar{q}_i = h_i^{-\theta}. \tag{25}$$

The actual output q_i of a craftsman cannot exceed the average potential output $\bar{q} = \mathbb{E}(\bar{q}_i)$ in the economy, so that:

$$q_i = \min\{\bar{q}_i, \bar{q}\}. \tag{26}$$

The assumption that individual productivity is constrained by aggregate knowledge is not essential to any of our results. Still, without this assumption in any period there would be some masters with arbitrarily high output, which is implausible. With the constraint, a good part of the knowledge in the economy is latent knowledge that will unfold its full potential only in later generations. This closely relates to Mokyr (2002)'s argument that the growth of productivity is constrained by the epistemic base on which a technique rests. The more people using a technique understand the science behind it, the broader the base. According to Mokyr (2002), this basis was very narrow in pre-modern Europe and gradually became wider.

Figure 7 illustrates the distribution of actual output q_i among craftsmen for two values of knowledge k, where the dashed line corresponds to a higher state of knowledge. The kinks in the distribution functions represent the points above which potential productivity is constrained by the average knowledge in the society. Because of the specific shape of the exponential distribution, the share of craftsmen who are constrained by the average knowledge is constant (and given by $1/e$).
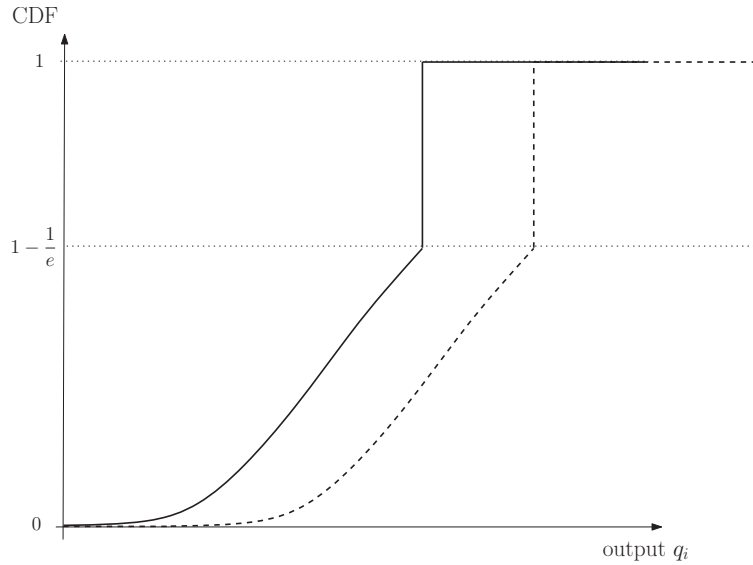

Figure 7: Distribution Function of Productivity at time t (solid line) and $t' > t$ (dashed line)

Given the exponential distribution for h_i and (25), potential output $\bar{q}_i$ follows a Fréchet distribution with shape parameter $1/k$ and scale parameter $1/\theta$.

We can now express the total supply of effective labor by craftsmen as a function of state variables. The average potential output across craftsmen is given by:

$$\bar{q} = \int_0^\infty h_i^{-\theta} \left(k \exp(-kh_i)\right) dh_i = \int_0^\infty k^\theta (kh_i)^{-\theta} \exp(-kh_i) \, kdh_i = k^\theta \Gamma(1-\theta),$$

where $\Gamma(t) = \int_0^\infty x^{t-1} \exp(-x) dx$ is the Euler gamma function. Given (26), the actual output q_i of a craftsman is:

$$q_i = \min\{\bar{q}_i, \bar{q}\} = \min\left[h_i^{-\theta}, k^\theta \Gamma(1-\theta)\right].$$

The threshold for h_i below which craftsmen are constrained by average knowledge is given by:

$$\hat{h} = k^{-1} \Gamma(1-\theta)^{-1/\theta}.$$

The expected supply of output of a given craftsman is:

$$\mathbb{E}(q_i) = \int_0^{\hat{h}} k^\theta \Gamma(1-\theta) k \exp[-kh_i] dh_i + \int_{\hat{h}}^\infty h_i^{-\theta} k \exp[-kh_i] dh_i$$
$$= k^\theta \Lambda.$$

Here Λ is a constant given by:

$$\Lambda = \Gamma(1-\theta) + \exp[-\Gamma(1-\theta)^{-1/\theta}] \theta \Gamma(-\theta) + \Gamma(1-\theta, \Gamma(1-\theta)^{-1/\theta}),$$

and $\Gamma(t,s) = \int_s^\infty x^{t-1} \exp(-x) dx$ is the incomplete gamma function. The total supply of craftsmen's labor L in efficiency units is then given by the expected output per craftsmen $\mathbb{E}(q_i)$ multiplied by the number of craftsmen N:

$$L = N k^\theta \Lambda.$$

In sum, all the results in the benchmark continue to hold with the "Leonardo" assumption, up to some constant terms: $\Gamma(1-\theta)$ should be replaced by Λ.

In the proof of Proposition 3, the "Leonardo" assumption requires to compute $\partial \mathbb{E}(q')/\partial k'$ differently. In particular, in deriving $\mathbb{E}(q')$ with respect to k' we should be careful in taking as given the future average society knowledge $\bar{q}' = (k')^\theta \Gamma(1-\theta)$, i.e. the externality in (26). More precisely, (26) should be written as:

$$\mathbb{E}(q') = \int_0^{\hat{h}'} \underbrace{(k')^\theta \Gamma(1-\theta)}_{\bar{q} \text{ (exogenous)}} k' \exp[-k'h_i] dh_i + \int_{\hat{h}'}^\infty h_i^{-\theta} k' \exp[-k'h_i] dh_i$$

where

$$\hat{h}' = \Gamma(1-\theta)^{-1/\theta}/k'.$$

Integrating we obtain:

$$\mathbb{E}(q') = (1 - \exp[\Gamma(1-\theta)/\theta])\,\bar{q} + (k')^\theta\,\Gamma(1-\theta,\Gamma(1-\theta)^{-1/\theta})$$

and the derivative is

$$\frac{\partial\mathbb{E}(q')}{\partial k'} = \theta\Gamma(1-\theta,\Gamma(1-\theta)^{-1/\theta})(k')^{\theta-1} = \Theta(k')^{\theta-1}.$$

with $\Theta = \theta\Gamma(1-\theta,\Gamma(1-\theta)^{-1/\theta})$. Compared to the benchmark, there is a factor $\Gamma(1-\theta,\Gamma(1-\theta)^{-1/\theta})$ instead of a factor $\Gamma(1-\theta)$.

C   Proof of Proposition 2

The threshold for sufficient altruism is given by

$$\hat{\gamma} = \frac{(\delta(n^{\text{F}}) - \kappa n^{\text{F}})\,\bar{n}s}{(1-\alpha)(n^{\text{F}})^2}\Gamma(1-\theta), \quad \text{with } n^{\text{F}} = (1+\nu)^{\frac{(1-\alpha)\theta}{\alpha}}.$$

We claim that the balanced growth path exists if $\gamma > \max\{0, \hat{\gamma}\}$.

Let us first compute the balanced growth path, supposing it exists. The growth rate of knowledge in (b) comes from (13) where we have imposed $m = m^{\text{F}} = 1$. Population growth is obtained using (10). Income per capita in (c) derives from (9). Utility in (d) is derived as follows: Income of a given craftsman is $q_i\,(1-\alpha)\frac{Y}{L} + \kappa a^{\text{F}}$ (from (5)). Expected income, using (6), is $k^\theta\Gamma(1-\theta)(1-\alpha)\frac{Y}{L} + \kappa a^{\text{F}} + \alpha y^{\text{F}}$, where αy^{F} is income from owning land. Given the value of L from (7), this simplifies into $(1-\alpha)\frac{Y}{N} + \kappa a^{\text{F}} + \alpha y^{\text{F}}$. The future labor income of the child is $(1-\alpha)y^{\text{F}}$.

For the balanced growth path defined above to be incentive compatible, i.e. parents are indeed willing to provide their kids with teaching, the cost of teaching should be less than the gain in the income, as evaluated by the altruistic parents. Normalizing the labor income of a craftsman without training to zero, this condition is:

$$\delta(n^{\text{F}}) - \kappa n^{\text{F}} < \gamma\,n^{\text{F}}E\left[(1-\alpha)q\frac{Y}{L}\right] = \gamma\,n^{\text{F}}(1-\alpha)y^{\text{F}}.$$

Using (6) and (7), this condition determines a lower bound on the altruism factor γ:

$$\hat{\gamma} > \frac{(\delta(n^{\text{F}}) - \kappa n^{\text{F}})\,\bar{n}s}{(1-\alpha)(n^{\text{F}})^2}\Gamma(1-\theta).$$

D Proof of Proposition 3

The required threshold for altruism is given by:

$$\gamma > \frac{\delta'\left((1+v)^{\frac{(1-\alpha)\theta}{\alpha}}\right) - \kappa}{\frac{(1-\alpha)v\theta}{\bar{n}s}(1+v)^{\frac{(1-\alpha)\theta}{\alpha} - 2}}.$$

Let us first compute the balanced growth path, supposing it exists. To determine the number of apprentices per master, we use (14). Equation (15) is derived as follows. Each apprentice learns from $m^c = (n^c)^o$ masters. As the draws for the initial knowledge of masters are not independent (all these masters were educated by the same persons), their acquired knowledge k^i is the same, but they had different ideas on their own drawn from $\text{Exp}(vk_{-1})$. The acquired knowledge of the apprentices thus follows:

$$(k^i)' = k^i + m^c vk_{-1}.$$

The final knowledge of the apprentices is given by

$$k' = (k^i)' + vk.$$

Using $(k^i)' = k' - vk$ and $(k^i) = k - vk_{-1}$ in the first equation, we get

$$k' - vk = k - vk_{-1} + m^c vk_{-1} \tag{27}$$

which leads to (15) where $g = k'/k$.

The average utility expression takes into account the flows between master and apprentices. Adults are paid as masters by a^c parents the amount of $\delta'(a^c) - \kappa$. Their disutility net of income from apprentices is $\delta(a^c) - \kappa(a^c)$. They also pay as parents the same amount $\delta'(a^c) - \kappa$ for each of their children n^c to each of their master m^c. The balance is:

$$a^c(\delta'(a^c) - \kappa) - (\delta'(a^c) - \kappa) - m^c n^c(\delta'(a^c) - \kappa) = -(\delta(a^c) - \kappa a^c).$$

From Equation (15) and the value of n^c, the growth rate $g = g^c$ should satisfy:

$$g^2 - (1+v)g + v = vg^{\frac{(1-\alpha)\theta o}{\alpha}}. \tag{28}$$

The left hand side is a convex function $f_1(g)$, while the right hand side is a function of g and o, $f_2(g, o)$. Figure 8 represents these two functions for different sizes of the clan. At the minimum possible value of g, the left hand side is smaller than the right hand side:

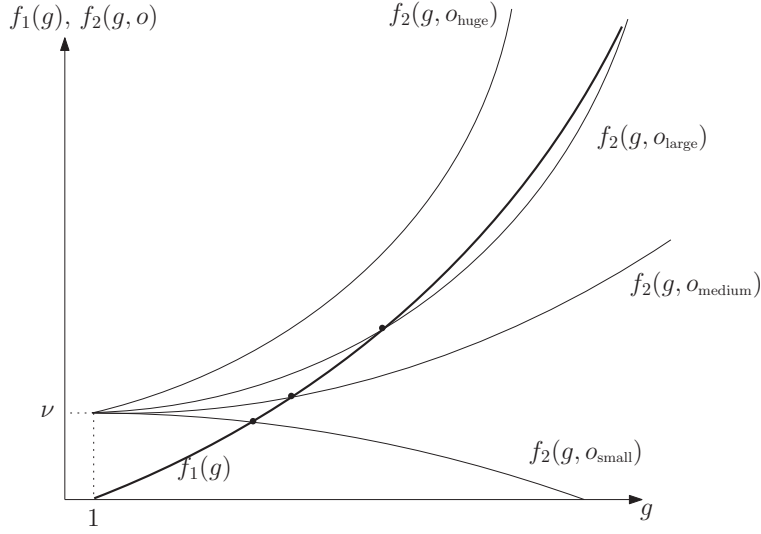$$f_1(1) = 0 < f_2(1, o) = v \forall o > 0.$$

Several cases may occur:

63

Figure 8: Equation (28)

- For $o \leq \frac{\alpha}{(1-\alpha)\theta}$, $f_2(g,o)$ is concave, crosses $f_1(g)$ once, and there exist a solution to the equality (28).
- For $\frac{\alpha}{(1-\alpha)\theta} < o \leq \frac{2\alpha}{(1-\alpha)\theta}$, one can apply the l'Hospital rule twice to show that

$$\lim_{g \to \infty} \frac{f_1(g)}{f_2(g,o)} > 1,$$

  implying that $f_2(g,o)$ is below $f_1(g)$ for large g and crosses it once. Hence there exist a solution to the equality (28).
- If $o > \frac{2\alpha}{(1-\alpha)\theta}$ but not "too large," $f_2(g,o)$ cuts $f_1(g)$ twice. There are two balanced growth paths.
- For o very large, the function $f_2(g,o)$ which is above $f_1(g)$ for $g = 1$, stays above it as g increases. In that case, there is no solution to Equation (28), and no balanced growth path. The interpretation is that the clan is so big that technological level and population grow at an accelerating rate.

We can summarize these findings by defining $\bar{o}$, such that if $o \leq \bar{o}$, a balanced growth path exists.

Differentiating (28), the effect of o on g is given by:

$$\frac{dg}{do} = \frac{\partial f_2 / \partial o}{\partial f_1 / \partial g - \partial f_2 / \partial g}.$$

The term $\partial f_2 / \partial o$ is positive as $g > 1$. We conclude that increasing o increases g for equilibria where $\partial f_1 / \partial g > \partial f_2 / \partial g$, that is where $f_2(g,o)$ cuts $f_1(g)$ from above as g increases.

64

Let us now consider whether such an equilibrium is incentive compatible. If o is too low, the threat of punishment is insufficient to prevent shirking, and only the family equilibrium exists. If o is large, parents may no longer be willing to apprentice their children with all current adult members of the clan. In other words, the clan should be large enough for the threat of punishment to ensure compliance, but small enough for parents to be willing to pay the apprenticeship fee. Hence, there exists thresholds $o_{\min}$ and $o_{\max}$ such that if $o_{\max} > o > o_{\min}$ the clan equilibrium is incentive compatible.

Assuming that the punishment technology is such that one person can do only negligible harm to another, but more than one person can exert a much more damaging action, sufficient in any case to deter shirking, we get $o_{\min} = 0$.[38] Let us now consider $o_{\max}$.

The clan equilibrium is sustained if, for each child, the marginal cost paid to the master is lower than the expected marginal benefit, as priced by the parents:

$$\delta'(a) - \kappa \leq \gamma \frac{\partial \mathbb{E}(q')}{\partial k'} \frac{\partial k'}{\partial m} (1 - \alpha) \frac{Y'}{L'}. \tag{29}$$

The right hand side represents the expected effect on individual productivity of meeting an additional master. $(1 - \alpha)\frac{Y'}{L'}$ is exogenous for the individual, and the altruism parameter γ reflects that the marginal benefit is seen from the point of view of the parent.

Let us first consider the term $\partial \mathbb{E}(q')/\partial k'$. From (6), the derivative is

$$\frac{\partial \mathbb{E}(q')}{\partial k'} = \theta \Gamma (1 - \theta)(k')^{\theta - 1}.$$

The term $\partial k'/\partial m$ can be directly obtained using (27) and is equal to vk_{-1}. Finally, the term Y'/L' can be transformed into:

$$\frac{Y'}{L'} = \frac{Y'}{N'}\frac{N'}{L'} = \frac{Y'}{N'}\frac{1}{\Gamma(1 - \theta)(k')^{\theta}} \tag{30}$$

using (7). Condition (29) can now be rewritten as:

$$\delta'(a) - \kappa \leq \gamma \theta (k')^{\theta - 1} vk_{-1} (1 - \alpha)\frac{Y'}{N'}\frac{1}{(k')^{\theta}}. \tag{31}$$

which, along a balanced growth path, reduces to

$$\delta'\left((g^{\mathrm{c}})^{\frac{(1-\alpha)\theta(o+1)}{\alpha}}\right) - \kappa \leq \frac{\gamma(1 - \alpha)v\theta}{\bar{n}s} (g^{\mathrm{c}})^{\frac{(1-\alpha)\theta}{\alpha} - 2}.$$

The left hand side is increasing in o as $g^{\mathrm{c}} > 1$, g^{c} is increasing in o, and $\delta(a)$ is convex. If it is smaller than the right hand side for the minimum value of o ($o = 0$, $g^{\mathrm{c}} = 1 + v$), i.e.

---

[38]Considering o as a continuous variable

if

$$\delta' \left((1+v)^{\frac{(1-\alpha)\theta}{\alpha}} \right) - \kappa < \frac{\gamma(1-\alpha)v\theta}{\bar{n}s}(1+v)^{\frac{(1-\alpha)\theta}{\alpha}-2}.$$

then either the right hand side becomes larger than the left hand side for some value of $o = \hat{o} > 0$, or they never intersect, in which case $\hat{o}$ is infinite. Notice that the right hand side is decreasing in g^c, and hence in o, provided that

$$(1-\alpha)\theta < 2\alpha,$$

in which case, $o_{\max}$, the maximum size of the clan which is incentive compatible, is necessarily finite.

In the analysis of the incentive compatibility, we have assumed that g^c was defined, we show above that it is not the case $o > \bar{o}$. Hence, the threshold above which a balanced growth path exists and is incentive compatible is $o_{\max} = \min\{\bar{o}, \hat{o}\}$.

E   Proof of Lemma 1

The first-order condition for the parent's problem can be written as:

$$\underbrace{p}_{\text{marginal cost}} n = \gamma\, n\, \underbrace{\frac{\partial\mathbb{E}\,(q')}{\partial k'}\frac{\partial\mathbb{E}\,(k')}{\partial m}(1-\alpha)\frac{Y'}{L'}}_{\text{marginal benefit }(\partial I'/\partial m)}.$$

Remembering from (6) that

$$\frac{\partial\mathbb{E}\,(q')}{\partial k'} = \theta\Gamma(1-\theta)(k')^{\theta-1},$$

and using $k' = k(m+v)$ (from (13)) as masters are now drawn randomly, we obtain, in equilibrium:

$$\delta'(a) - \kappa = p = \gamma\theta\Gamma(1-\theta)\frac{(k')^\theta}{m+v}(1-\alpha)\frac{Y'}{L'}.$$

Using (7), this equation simplifies into

$$\delta'(a) - \kappa = \gamma\theta(1-\alpha)\frac{1}{m+v}\frac{Y'}{N'}.$$

F   Proof of Proposition 4

For a fixed number of masters m, the market equilibrium yields higher growth in productivity because those masters are drawn randomly. Indeed, from the proof of Proposition 3, productivity in **C** follows

$$k' = (1+v)k + (m-1)vk_{-1}$$

66

which implies a growth rate equal to:

$$g^c = \frac{1 + v + \sqrt{(1+v)^2 + 4(m-1)v}}{2}$$

which is always less than the growth rate with the market, $m + v$, for $v > 0$ and $m > 1$.

Moreover, the equilibrium number of masters m^M is higher in the market equilibrium compared to the clan equilibrium. Indeed, m^M balances marginal cost and benefit. If the clan equilibrium had a higher number of masters, it would not be incentive compatible (parents would not like to pay all those masters).

Notice that, in the computation of the utility, the payments from apprentices, pa^M, and for children, $pn^M m^M$, balance.

G   Proof of Lemma 2

The maximization problem of the guild is:

$$\max_{a_j} \left\{ p_j a_j - \delta(a_j) + \kappa a_j \right\}$$

subject to:

$$
\begin{aligned}
S_j N' m_j &= N a_j, & (32) \\
p_j &= \gamma \frac{\partial EI'_{ij}}{\partial m_j}, \\
\gamma EI'_{ij} - p_j m_j &= \gamma(1-\alpha)\frac{Y'}{N'} - pm.
\end{aligned}
$$

Replacing p_j and p by their value from the second constraint into the third leads to:

$$\gamma (S'_j)^{\frac{1}{\lambda}-1}\left(\frac{k'_j}{k'}\right)^{\frac{\theta}{\lambda}} - \frac{\theta}{m_j+v}(S'_j)^{\frac{1}{\lambda}-1}\left(\frac{k'_j}{k'}\right)^{\frac{\theta}{\lambda}} m_j = \gamma - \frac{\theta}{m+v}m.$$

which can be solved for S'_j:

$$S'_j = \left[\frac{(\gamma-\theta)m + \gamma v}{(\gamma-\theta)m_j + \gamma v}\left(\frac{m_j+v}{m+v}\right)^{1-\frac{\theta}{\lambda}}\right]^{\frac{\lambda}{1-\lambda}}.$$

The second constraint can be rewritten as:

$$p_j = \gamma\theta(1-\alpha)\frac{1}{m+v}\frac{Y'}{N'}\frac{(\gamma-\theta)m+\gamma v}{(\gamma-\theta)m_j+\gamma v}$$

and the equilibrium on the apprenticeship market (32) is:

$$a_j = n \, S'_j \, m_j.$$

These constraints imply that lowering the supply of apprenticeships a_j increases the price p_j. It is now easier to express the maximization program in terms of m_j:

$$\max_{m_j} \left\{ \left(\frac{\gamma\theta(1-\alpha)}{m+v} \frac{Y'}{N'} \frac{(\gamma-\theta)\, m + \gamma v}{(\gamma-\theta)\, m_j + \gamma v} + \kappa \right) n \, S'_j \, m_j - \delta \left(n \, S'_j \, m_j \right) \right\}.$$

The first order condition is:

$$- (\gamma - \theta) \left(\frac{\gamma\theta(1-\alpha)}{m+v} \frac{Y'}{N'} \frac{(\gamma-\theta)\, m + \gamma v}{((\gamma-\theta)\, m_j + \gamma v)^2} \right) S'_j \, m_j +$$

$$\left(\left(\frac{\gamma\theta(1-\alpha)}{m+v} \frac{Y'}{N'} \frac{(\gamma-\theta)\, m + \gamma v}{(\gamma-\theta)\, m_j + \gamma v} + \kappa \right) - \delta' \left(n \, S'_j \, m_j \right) \right) \left(\frac{\partial S'_j}{\partial m_j} m_j + S'_j \right) = 0$$

with

$$\frac{\partial S'_j}{\partial m_j} = \frac{\lambda}{1-\lambda} \left[\frac{(\gamma-\theta)\, m + \gamma v}{(\gamma-\theta)\, m_j + \gamma v} \left(\frac{m_j + v}{m + v} \right)^{1-\frac{\theta}{\lambda}} \right]^{\frac{\lambda}{1-\lambda} - 1}$$

$$\times \left(-(\gamma - \theta) \frac{(\gamma-\theta)\, m + \gamma v}{((\gamma-\theta)\, m_j + \gamma v)^2} \left(\frac{m_j + v}{m + v} \right)^{1-\frac{\theta}{\lambda}} \right.$$

$$\left. + \left(1 - \frac{\theta}{\lambda} \right) \frac{(\gamma-\theta)\, m + \gamma v}{(\gamma-\theta)\, m_j + \gamma v} \left(\frac{m_j + v}{m + v} \right)^{-\frac{\theta}{\lambda}} \right).$$

At the symmetric Nash equilibrium between guilds, this becomes:

$$- (\gamma - \theta) \left(\frac{\gamma\theta(1-\alpha)}{m+v} \frac{Y'}{N'} \frac{1}{(\gamma-\theta)\, m + \gamma v} \right) m +$$

$$\left(\left(\frac{\gamma\theta(1-\alpha)}{m+v} \frac{Y'}{N'} + \kappa \right) - \delta' \left(n \, m \right) \right) \left(\frac{\partial S'_j}{\partial m_j} m + 1 \right) = 0$$

with:

$$\frac{\partial S'_j}{\partial m_j} = \frac{\lambda}{1-\lambda} \left(\frac{-(\gamma-\theta)}{(\gamma-\theta)\, m + \gamma v} + \left(1 - \frac{\theta}{\lambda} \right) \right),$$

68

which we can rearrange into:

$$\frac{\gamma\theta(1-\alpha)}{m+\nu}\frac{Y'}{N'}\left(\frac{-(\gamma-\theta)\,m}{(\gamma-\theta)\,m+\gamma\nu}+\frac{\partial S_j'}{\partial m_j}\,m+1\right)+(\kappa-\delta'\,(n\,m))\left(\frac{\partial S_j'}{\partial m_j}\,m+1\right)=0$$

and finally:

$$\delta'(nm)-\kappa=\left(\frac{\gamma\theta(1-\alpha)}{m+\nu}\frac{Y'}{N'}\right)\Omega(m)$$

with:

$$\Omega(m)=\frac{\left(\frac{-(\gamma-\theta)m}{(\gamma-\theta)m+\gamma\nu}+1+\frac{\lambda m}{1-\lambda}\left(\frac{-(\gamma-\theta)}{(\gamma-\theta)m+\gamma\nu}+\left(1-\frac{\theta}{\lambda}\right)\right)\right)}{1+\frac{\lambda m}{1-\lambda}\left(\frac{-(\gamma-\theta)}{(\gamma-\theta)m+\gamma\nu}+\left(1-\frac{\theta}{\lambda}\right)\right)}.$$

$\Omega(m)$ can be further simplified into:

$$\Omega(m)=\frac{1-\lambda+(\lambda-\theta)m-\frac{(\gamma-\theta)m}{(\gamma-\theta)m+\gamma\nu}}{1-\lambda+(\lambda-\theta)m-\lambda\frac{(\gamma-\theta)m}{(\gamma-\theta)m+\gamma\nu}}.$$

When $\lambda\to1$, $\frac{\partial S_j'}{\partial m_j}\to\infty$ and $\Omega(m)\to1$.

H   Proof of Proposition 5

Before considering the optimization problem, let us compute the effect of changing m_j on income I_j. Using Equation (7), we can compute the relative quantity of efficient labor in sector j as:

$$\frac{L_j'}{L'}=S_j'\left(\frac{k_j'}{k'}\right)^{\theta}.$$

With this expression, and with Equation (6), which adapts to trade j as $Eq_j=\Gamma(1-\theta)k_j^{\theta}$, it is convenient to rewrite expected income as:

$$EI_{ij}'=(1-\alpha)\frac{Y'}{N'}(S_j')^{\frac{1}{\lambda}-1}\left(\frac{k_j'}{k'}\right)^{\frac{\theta}{\lambda}}.$$

Let us now compute the effect of changing m_j on individual income. Using the result in (30), and $k_j'=(m_j+\nu)k_j$, we get:

$$\frac{\partial EI_{ij}'}{\partial m_j}=\theta\Gamma(1-\theta)\frac{(k_j')^{\theta}}{m_j+\nu}(1-\alpha)\frac{Y'}{L'}\left(\frac{L_j'}{L'}\right)^{\frac{1}{\lambda}-1}$$

which can moreover be simplified into, using (30):

$$\frac{\partial EI'_{ij}}{\partial m_j} = \theta(1 - \alpha)\frac{(k'_j)^\theta}{(k')^\theta}\frac{1}{m_j + v}(1 - \alpha),$$

leading to:

$$\frac{\partial EI'_{ij}}{\partial m_j} = \theta(1 - \alpha)\frac{1}{m_j + v}\frac{Y'}{N'}(S'_j)^{\frac{1}{\lambda} - 1}\left(\frac{k'_j}{k'}\right)^{\frac{\theta}{\lambda}}.$$

Marginal income is therefore equal to expected income multiplied by: $\frac{\theta}{m_j + v}$.

To study the equilibrium, one should consider Equation (24) replacing a^G, m^G and y^G by their value:

$$\delta'((g^G - v)n^G) - \kappa = \gamma\theta(1 - \alpha)\frac{1}{g^G}\frac{n^G}{\bar{n}s}\Omega(g^G - v). \tag{33}$$

This equation describes a relationship between g^G and n^G which we call the "apprenticeship monopolistic market," as it is derived from the demand for apprenticeship and the monopolistic behavior of the guild. Equation (33) can be rewritten as:

$$n^G = \frac{\kappa}{\bar{\delta}(g^G - v) - \dfrac{\gamma\theta(1 - \alpha)}{s\bar{n}\,g^G}\Omega(g^G - v)}.$$

If we compare this expression with the equivalent in the market equilibrium, Equation (20), we see that the denominator is necessarily larger. Hence, for any given g, $n^G < n^M$. It follows that $g^G < g^M$.

Notice finally that, as in the market equilibrium, the payments from apprentices, pa^G, and for children, $pn^G m^G$, balance in the computation of the utility.

I   Proof of Proposition 6

We can compute the gains of adopting the guild institution as:

$$\begin{aligned}
u^{F\to G} - u^{F\to F} &= \gamma n_0(y_1^G - y_1^F) + \kappa(a_0 - n_0) - \delta(a_0) + \delta(n_0) - \mu(N_0),\\
u^{C\to G} - u^{C\to C} &= \gamma n_0(y_1^G - y_1^C) + \kappa(a_0 - (n_0)^{o+1}) - \delta(a_0) + \delta((n_0)^{o+1}) - \mu(N_0).
\end{aligned}$$

$\underline{N}$ makes people in the family equilibrium indifferent between adopting the guild or not, i.e., it solves:

$$\gamma n_0(y_1^G - y_1^F) + \kappa(a_0 - n_0) - \delta(a_0) + \delta(n_0) - \mu(\underline{N}) = 0.$$

One should show that for $N_0 = \underline{N}$, people in the clan equilibrium do not want to adopt the guild, i.e.:

$$\gamma n_0 (y_1^G - y_1^C) + \kappa(a_0 - (n_0)^{o+1}) - \delta(a_0) + \delta((n_0)^{o+1}) - \mu(\underline{N}) < 0.$$

This is true if:

$$\gamma n_0 y_1^C + (\kappa(n_0)^{o+1} - \delta((n_0)^{o+1})) > \gamma y_1^F + \kappa n_0 - \delta(n_0). \qquad (34)$$

Let us define the following function:

$$\psi(m) = \gamma n_0 u(m) + \kappa m n_0 - \delta(m n_0).$$

$u(m)$ is the function that relates future income to number of masters learning from, in the context of the clan equilibrium. From (8) and (27), we get:

$$u(m) = \Gamma(1 - \theta)^{1-\alpha} \underbrace{((1+v)k - vk_{-1} + mvk_{-1})}_{k'}{}^{(1-\alpha)\theta} (N')^{-\alpha}.$$

Hence, $u(m)$ is increasing and concave in m. As a consequence, $\psi(m)$ is also concave in m ($\delta(\cdot)$ is convex). To see whether it is increasing, we can compute:

$$\psi'(m) = \gamma \, n_0 (1 - \alpha) \Gamma(1 - \theta)^{1-\alpha} \theta(k')^{(1-\alpha)\theta-1} v k_{-1} (N')^{-\alpha} + \kappa n_0 - \delta'(m n_0) n_0.$$

We also know from Appendix D that the clan equilibrium is sustained if the marginal cost paid to the master is less than the expected marginal benefit, i.e. $\delta'((n_0)^{o+1}) - \kappa \le \partial y_1^C / \partial m_0$, which implies, from (31) and (8):

$$\gamma \theta \, (1 - \alpha) \Gamma(1 - \theta)^{1-\alpha} (k')^{(1-\alpha)\theta-1} v k_{-1} (N')^{-\alpha} + \kappa - \delta'(m n_0) \ge 0.$$

This individual level condition implies that, at the aggregate equilibrium, $\psi'(m) > 0$. Using the mean value theorem for derivatives, we know there exists $\tilde{m} \in [1, m^c]$ such that $(\psi(m^c) - \psi(1))/(m^c - 1) = \psi'(\tilde{m})$. As $\psi(\cdot)$ is concave, $\psi'(\tilde{m}) > \psi'(m^c) > 0$ which proves $\psi(m^c) > \psi(1)$ and inequality (34) holds.

$\overline{N}$ makes people in the clan equilibrium indifferent between adopting the guild or not, i.e. it solves

$$\gamma n_0 (y_1^G - y_1^C) + \kappa(a_0 - (n_0)^{o+1}) - \delta(a_0) + \delta((n_0)^{o+1}) - \mu(\overline{N}) = 0.$$

One should show that for $N_0 = \overline{N}$, people in the family equilibrium also want to adopt the guild, i.e.:

$$\gamma n_0 (y_1^G - y_1^F) + \kappa(a_0 - n_0) - \delta(a_0) + \delta(n_0) - \mu(\overline{N}) > 0.$$

This is true as $\mu(\overline{N}) < \mu(\underline{N})$.